ABSTRACT

Static electrical conductivity (SEC) and dielectric measurements were made on Antarctic ice cores at -15°C. The observed behaviour is markedly different from that of temperate glacier ice. The influence of impurities on the electrical properties of polar ice is discussed. Variations of SEC do not appear to be correlated with variations in the relaxation frequency when the loss factor is maximal. Different growth conditions coupled to ageing effects in the first few metres of the firm may explain variations in the electrical properties along an ice core. Moreover, it is suggested that the relaxation frequency increases as the specific surface area increases. Defects are produced in the firm near the surface and may be retained in the subsequent ice. Discontinuous changes in the high-frequency electrical conductivity between adjacent layers can induce internal reflections of radio waves within ice sheets.

INTRODUCTION

Polar ice exhibits electrical properties which are very different from those of pure artificial ice or temperate glacier ice. The static electrical conductivity (SEC) of cold polar ice is typically $10^{-5}$ S m$^{-1}$ compared to $10^{-8}$ S m$^{-1}$ in temperate glacier ice. At a given temperature, the frequency corresponding to the maximum absorption of the Debye dispersion is similar to that of the HF-doped ices. A review of the dielectric properties of Antarctic ice was given by Glen and Paren (1975) and Fitzgerald and Paren (1975). Similar results were obtained by mechanical damping measurements (Vassoi11e and others 1980 and 1982). The influence of impurities found in polar ice was compared with laboratory-doped ices (Paren 1973, Fitzgerald and others 1977). But, as shown by Shaw (1979), most impurities in the snow of the Antarctic plateau are microparticles (Aitken particles, sea-salt particles). Even if these particles are dissociated in firn, the influence of such impurities is difficult to assess. Moreover the content of impurities in polar ice is generally low. However a good correlation between SEC and acidity was found by Hammer (1980) in Greenland ice and between SEC and sulphate content by Maccagnan and others (1981) in the Dome C ice core, East Antarctica. It is possible that variations of SEC are induced by impurities and that the background values of polar ice are induced by other mechanisms. Fitzgerald and others (1977) and Vassoi11e and others (1980) have suggested that ageing of firn has an effect on the electrical and mechanical behaviour of polar ice. This theory will be discussed in this paper, based on electrical measurements on Antarctic ice cores. The origin of radio echo layers observed within the Antarctic ice sheet will be also discussed in relation to variations in the ice conductivity. An explanation for the disappearance of internal reflections near the bedrock of ice sheets is also given.

1. EXPERIMENTAL METHODS

1.1. Conductivity measurements along an ice core

Two flat faces are cut parallel to the axis of the core. An assembly of electrodes is then scratched along the core, the applied voltage being 250 V. The current is amplified and recorded. The electrodes are made of seven independent contacts, and the cathode is surrounded by a guard ring. The sliding speed of the electrodes is 5 mm s$^{-1}$ or 25 mm s$^{-1}$ and the temperature is -15°C. Since the exact contact area of the electrodes with ice and the geometry of currents are unknown, and since it was not verified that the current was proportional to voltage, we cannot derive quantitative values of the conductivity; we can only record the current through the ice core. Measurements are reproducible, provided that a fresh surface is cut shortly before the experiments.

1.2. Dielectric measurements

Samples were cut from ice cores 100 mm in diameter. The flat faces of the samples were cut with a microtome and the diameter with a band saw. These operations were done in a cold room (temperature -16°C). The dimensions of the samples were 70 mm in diameter and about 7 mm in thickness.

The samples were then placed in the dielectric cell and allowed to rest for at least 3 h, under a moderate pressure of the electrodes. The dielectric cell was a cell with two silver-plated electrodes and without a guard ring (the relative importance of surface current is minor for a wide sample). Measurements were made with a General Radio capacitance measurement assembly 1620 A or a Hewlett Packard vector impedance meter 4800 A.

Some measurements were also done on pure ice samples, the dielectric behaviour of which is well known. The values found for the low frequency permittivity and the relaxation time suggest an air gap of about 0.03 mm between the sample and the electrodes. Some corrections were made on the measurements on polar ice in order to take into account the influence of this air gap (Maccagnan unpublished).
2. RESULTS

2.1. Dome C

SEC was measured on an ice core taken from a depth of about 601 m at Dome C, central Antarctica (74°39'S, 124°10'E, elevation: 3,240 m, mean annual temperature: -53.5°C).

The record of current shows large variations along this core: the minimum is about 0.1 µA and the maximum 0.9 µA (Fig.1). Two samples for dielectric measurements were chosen from the core: one in the less conductive part (680.96 m), and the other in the more conductive part (681.26 m). The real part of the conductivity at -15°C was plotted against frequency for both samples (Fig.2). The relaxation frequency, for which \( \sigma = 1/(2\sigma_S + \omega_m) \) is the same for both samples: 2.2 kHz after computation (\( \sigma_S \) is the low frequency conductivity and \( \omega_m \) the high frequency limiting conductivity).

2.2. D 10

SEC was measured on an ice core taken from a depth of about 46 m at D 10, a coastal site in Antarctica (66°40'S, 140°01'E, elevation 270 m, mean annual temperature: -13°C). The current was about 0.4 µA in the upper part of the core and 0.001 µA in the lower part (Maccagnan and others 1981). The current in the lower part was of the same order as that measured on temperate glacier ice cores or on artificial pure samples. Two samples of ice were taken for dielectric measurements: one from the upper part of the core and the other in the lower part. The real part of the conductivity is plotted against frequency for these samples at -15°C on Fig. 3. The relaxation frequency is 2.4 kHz for the sample 46.05 m and 19 kHz for the sample 46.10 m.

3. DISCUSSION

As shown in Figure 1, large variations of SEC are observed along the ice core studied. From Hammer (1980), a good relationship is found between SEC and the acidity of melted samples, provided that the H+ concentration is higher than 1 µequiv. H+ kg⁻¹. For the Dome C ice core, it is confirmed that most of the acid fallout is H₅SO₄ induced by volcanic eruptions (M Legrand personal communication). Since H₂SO₄ and H₂O show an eutectic with a low freezing point, sulphate can be found in a liquid phase at the grain boundaries. The high SEC values correlated with sulphate content could then be due to the existence of these liquid conducting paths (Maccagnan unpublished). But, according to Maccagnan and others (1981), the relation between SEC and sulphate content varies from core to core. Those authors explain this discrepancy in two ways: (i) variation of SEC with crystal-growth conditions in the first few metres of the firm; (ii) effect of ageing. Indeed, the static conductivity decreases with time for relatively good ice single crystals (Von Hippel and others 1972) and it decreases with ageing (Maidique and others 1971, Taubenberger 1973). But, as a consequence, ageing effects depend on growth conditions. Thus, large ageing effects are observed when small volumes of super-cooled water freeze (Evrad 1973). From Figure 2, no measurable variation of the relaxation frequency was observed for the two samples whereas large variations of SEC were observed (Fig.1). The high relaxation frequency found in the D 10 ice-core sample (Fig.3) for which the value of SEC was very small (Maccagnan and others 1981) clearly shows the effect of ageing. This assertion is supported by studies of ageing effects on the dielectric properties of ice formed by supercooling breakdown by Evrad (1973), Boned and Barbier (1973), and Lagourette (1976). At a given temperature, the low frequency conductivity decreases with time whereas the Debye relaxation frequency increases. It was verified by these authors that ageing effects were obtained within a short time provided that temperature was near the melting point and that the specific surface area in the ice was high. Moreover, from experiments on disperse microcrystals, Lagourette and others (1976) deduced that the frequencies at the maximum of the Debye dipolar absorption increased with specific surface area. Klivivdze and others (1974) pointed out that the mobility of the elements of the ice lattice increased as the size of the ice particles decreased.

Thus, changes in the relaxation frequency in the firm might be correlated with the specific surface area. If, due to low temperature, ageing ceases, a memory of the internal structure of ice may be kept. At Dome C, the temperature in the firm is lower than -50°C below 20 m (Ritz and others 1982) and so ageing cannot be efficient in modifying the ice structure. Thus, ageing effects can be invoked only in the first few metres of the firm in which temperature may rise up to -20°C during summer. With this assumption, changes in the dielectric behaviour along an ice core would be induced by changes in the specific surface area in the upper metres of the firm. Only crystal growth, as observed by Duval and Lorius (1980), can modify the ice structure down to 900 m at Dome C.

![Fig.1. Static electrical conductivity along an ice core (from the Dome C ice core). The current was measured at -15°C.](image1)

![Fig.2. Frequency dependence of conductivity of two samples from the Dome C ice core. Temperature: -15°C.](image2)

![Fig.3. Frequency dependence of conductivity of two samples from the D 10 ice core. Depth: 46 m, temperature: -15°C.](image3)
This point will be discussed in relation to the origin of the radio echo layers in polar ice masses.

4. RADIO ECHO LAYERS IN POLAR ICE SHEETS

4.1. Possible causes of layering

Internal reflections have been observed over wide areas of the Antarctic and Greenland ice sheets. According to Harrison (1973) differences in the dielectric constant between layers caused by the orientation of anisotropic crystals, or density variations, can explain echoes. Similar ideas were put forward by Ackley and Kelcher (1979) and Hammer (1980). Paren and Robin (1975) show that variations in the electrical conductivity can explain the deeper echoes.

By considering a simple model with a single boundary, the reflection coefficient $R$ is given by:

$$ R = \frac{A \Delta \sigma_{\text{sec}}}{E_0 \sigma_{\text{sec}}} $$

where $\Delta \sigma_{\text{sec}}$ is the variation of conductivity between two layers, $E_0$ the permittivity of free space, $\sigma_{\text{sec}}$ the dielectric constant at high frequencies, and $\omega$ the angular frequency.

If the dielectric behaviour of polar ice is described by two dispersions (the Debye dispersion and a low frequency dispersion), the electrical conductivity $\sigma_{\text{sec}}$ is given by:

$$ \sigma_{\text{sec}} = \sigma_0 + \sigma_1 \Delta \tau_1 + \sigma_2 \Delta \tau_2 $$

$\sigma_0$ is SEC, $\tau_1$ and $\tau_2$ are relaxation times, and $\Delta \tau_1$ and $\Delta \tau_2$ are the differences in permittivity at low and high frequencies, respectively.

**Fig.4.** Frequency dependence of conductivity of the Dome C ice core for different depths. Temperature: -15°C.

Figure 4 shows variations in conductivity with frequency for three samples of the Dome C ice core. The reflection coefficient calculated at -15°C for the extreme values of $\sigma_{\text{sec}}$ is about -68 dB for a single interface.

Variations of $\sigma_{\text{sec}}$ may be caused by (i) variations in $\sigma_0$ (SEC), (ii) variations in the strength of the Debye dispersion in conductivity, and (iii) variations in the strength of the second dispersion in conductivity. These three possibilities are investigated.

(i) Variations in $\sigma_0$.

As discussed previously in this paper, high values of SEC are found in polar ice, and variations of SEC are also observed (Fig.1) (Hammer 1980). The variation of $\sigma_{\text{sec}}$ observed in Figure 2 seems to be caused by the variation of SEC in the two samples studied. The corresponding reflection coefficient between the two samples is about -71 dB at -15°C.

(ii) Variations in the strength of the Debye dispersion.

Differences in the Debye conductivity at high frequency may be due to variations in $\Delta \tau_1$ and $\tau_1$.

The impurity level in polar ice is probably too low to induce significant variations in SEC. In Figure 3, the large variation in $\sigma_{\text{sec}}$ is clearly caused by a variation in the relaxation time between the two samples studied. The reflection coefficient calculated at -15°C is -56 dB.

Paren and Robin (1975) considered the reflection coefficient for the boundary between pure and polar ice. Differences in $\sigma_{\text{sec}}$ were almost entirely due to variations in the activation energy. Differences in relaxation times, at a given temperature, can also result in different values of the pre-exponential factor of the Arrhenius law. The very high relaxation frequency found for a sample of the D10 ice core (Fig.3), compared to that of Dome C ice samples, cannot be explained by variations in the activation energy. As discussed previously, only high impurity content or ageing effects may explain this particular behaviour. The very low value of SEC found for this sample by Maccagnan and others (1981) supports the assumption concerning ageing effects.

For a similar activation energy, the relaxation frequency of dispersed crystals seems to increase with the specific surface area (Lagourette and others 1976). A high relaxation frequency might be found in ice samples (with negligible specific surface area) provided that the memory of the physical state of ice in the firm is kept. With this assumption, radio echo layers might reflect variations in the ageing conditions or variations in the specific surface area in the first metres of the firm. As discussed above, the former depends on the latter.

(iii) Variations in the strength of the second dispersion.

A low frequency relaxation, which was observed in polar ice samples by Maeno (1974), gives very high values for the dielectric constant (>1000) at low frequency. The origin of this dispersion is not clear (possibly caused by polarization due to space charges or mechanical strains). Thus, at this stage, it is difficult to assess the part played by this dispersion in the internal reflections.

4.2. Cause of the disappearance of internal reflections within the lowest few hundred metres of ice sheets

From radio echo profiles given by Robin and others (1977) and that given in Figure 5, it appears that no layer is detected within the last few hundred metres of ice sheets. The separation between the deepest visible layer and bedrock changes with the ice location. On the other hand, there is some indication of reduced SEC above the bedrock (Glen and Paren 1975). The influence of higher temperature coupled with effects of strain leading to recrystallization was put forward by Glen and Paren (1975). From the crystalline texture in the Byrd ice core given by Gow and Williamson (1978), and in the Dome C ice core by Duval and Lorius (1980), only crystal growth induced by the grain boundary free energy is observed in the top layers of cold ice sheets. With this mechanism, no crystal nucleation occurs; only the bigger crystals grow at the expense of the smaller ones. Thus,
the memory of growth conditions and ageing effects in the firm can be retained. But, from the study of Gow and Williamson (1976), dynamic recrystallization must occur below 1800 m when the temperature is higher than approximately -13°C. With this recrystallization mechanism, crystal growth is also observed but new grains are created. Thus, the memory effect of the internal structure of ice crystals in the firm should be cancelled by extensive recrystallization. Since the cumulative strain for deep ice (at about 1800 m in the Byrd ice core) is probably higher than 100% (Duval and Le Gac 1982), the critical strain for recrystallization is attained above the maximum depth at which layers are detected. Thus, only temperature can be invoked to explain the disappearance of internal reflections above the bedrock. As a consequence, the line below which no visible layer is detected is probably an isothermal line.

ACKNOWLEDGEMENTS

We thank L. Philippe and A. Challiou for their important participation in the experimental work and M. Legrand and R. Delmas for valuable discussions. Field work was supported by Terres Australes et Antarctiques Françaises, Expéditions Polaires Françaises, and the US National Science Foundation as a contribution to the International Antarctic Glaciological Project. D.J. Drewry is acknowledged for the radio echo profile at Dome C shown in Figure 5.

REFERENCES

Fitzgerald W J, Glen J W, Paren J G 1977 Are the anomalous dielectric properties of polar ice due to impurities? International Association of Hydrological Sciences Publication 118 (General Assembly of Grenoble 1976 – Isotopes and Impurities in Snow and Ice): 3-8
Gow A J, Williamson T 1976 Rheological implications of the internal structure and crystal fabrics of the West Antarctic ice sheet as revealed by deep core drilling at Byrd station. CRREL Report 76-35
Lagourette B 1976 Study of the dielectric properties of disperse micro-crystals of ice near the melting temperature. Section I: experimental results. Journal de Physique 37(7-8): 945-954
Ritz C, Lliboutry L, Rado C 1982 Analysis of a 870 m deep temperature profile at Dome C. Annals of Glaciology 3: 284-289