ELECTRICAL RESISTIVITY OF GEORGE VI ICE SHELF, ANTARCTIC PENINSULA

by

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ABSTRACT

A georesistivity survey was made on part of George VI Ice Shelf (71°55′S, 67°20′W). The principal objectives were to determine the electrical structure of the ice shelf, in particular how refrozen melt water differs in electrical behaviour from dry firn, and to investigate the environment beneath the ice shelf.

Apparent resistivity profiles using a Schlumberger electrode configuration have been interpreted using Ghosh's convolution method for vertical electrical sounding (VES), adapted for use where extreme resistivity contrasts are present.

Warm, wet surface conditions tend to reduce the gross resistivity of shallow permeable layers. The electrical results indicate that the refrozen free water has affected the resistivity only indirectly; the mean density of firn is raised to about 0.915 Mg m⁻³ within the uppermost 10 m of the ice shelf at which point the resistivity is comparable to that of ice of the same density but formed by compaction of firn. The apparent resistivities in the top 100 m reflect the variation of density with depth; a small range of resistivities implies that the range of density is narrow and that densification is affected by the percolation and refreezing of melt water.

The bulk of the ice behaves as if resistivity either is independent of temperature or has only a slight dependence (activation energy -0.15 eV) with a basal melting rate in excess of 1 to 2 m a⁻¹. The principal resistivities determined for two sites on George VI Ice Shelf were within 10% of those at station BC on the Ross Ice Shelf, allowing for differences in temperature. This indicates that polar ice, i.e. non-temperate ice, has a very narrow range of resistivity. The apparent resistivity profiles are consistent with there being sea-water of oceanic salinity under the ice shelf.

INTRODUCTION

There are six recent publications on Antarctic resistivity surveys (Bentley 1977, 1979, Bentley and others 1979, Shabtaie and Bentley 1979, Shabtaie and others 1980, Thyssen and Shabtaie 1980). The sites of these and earlier investigations, namely, Ross Ice Shelf, Roosevelt Island, McMurdo Ice Shelf, and Dome C, are cold, dry-surface environments. The present work was undertaken on the west side of the Antarctic Peninsula, an area far warmer than the other areas studied. The surface of George VI Ice Shelf undergoes extensive melting, leading to the formation of large melt-water lakes in summer (Reynolds 1981[b]).

This work was carried out along the line of an established survey network called the M scheme (71°55′S, 67°30′W, Fig.1), principally at two stake rosettes Juliet and Kilo, referred to hereafter as RJ1 and RK2, respectively. The main source of ice is Goodenough Glacier which flows towards Alexander Island from the Palmer Land plateau (Bishop and Walton 1981), a dry-snow environment with mean annual
FIELD MEASUREMENTS

A standard Schlumberger electrode configuration was used for all profiles. Current was provided by a bank of up to six 90 V dry cells. Stainless steel tubes 1 m in length and 19.05 mm in outside diameter were used as electrodes. To reduce the contact resistance the snow around the electrodes was soaked with a salt solution. The potential and current were monitored by Keithley 6028 electrometers which have an input impedance (for voltage measurements) greater than 10¹⁴ ohm. Plots of the mutual decay of voltage and current were obtained from the outputs of the electrometers on a Minigor 510 XY-Yt chart recorder. Calibration checks in the field showed that voltage and current displayed on the chart recorder were within ±2%.

One of the problems encountered was the presence of background electrical fields detected in the potential recording circuit. A quasi-static potential (Vb, up to 150 mV) was observed in the absence of an applied current. In addition, micropulsations were detected of the order of a few tens of millivolts in amplitude and at a frequency of 6 to 10 Hz. Lower frequency oscillations were also present. Although generally attributable to natural perturbations in the Earth's magneto-telluric field, some oscillations seemed to be more prevalent at times of high wind. This may be due to electrostatic charging of ground drift and/or wind-induced movement of the cables which were suspended at least 1 m above the snow surface. The varying level of background electrical noise was normally insufficient to stop measurements although at times it reduced their reliability. However, there were occasions when ground drift and blowing snow caused so much "white" noise that measurements were terminated.

Conduction of electricity in ice is by the movement of protons. They appear to be freely discharged from the ice at the cathode but become increasingly depleted at the anode. This results in an increased contact resistance and a reduction in current. When current is applied, the ground potential must decrease concurrently with the depletion of the applied current as Ohm's Law is obeyed in the bulk of the ice. The duration of the decay varied from about 10 s to several minutes, the latter being more common at large electrode spacings. It is this decay which was monitored in the experiments. Examples of the voltage-current graphs from the chart recorder were digitized and a linear regression analysis carried out. The gradient of the decay line R was substituted in Equation (1). In cases the decay was too small to be reliable or micropulsations reduced the resolution, the mean ground potential V and mean applied current I were used instead to determine a parameter R0 in place of ΔV/ΔI, where

\[ R_0 = \frac{V}{I}. \]

Figure 3 represents the various parameters which feature in the analysis. Vo is the potential extrapo-

\[ \text{(b)} \]

\[ \text{(a)} \]

\[ \text{Fig. 2. Examples of voltage-current decay graphs. See text for further details.} \]

\[ \text{Fig. 3. Details of the statistical parameters used.} \]

\[ \text{The voltage-current decay measured is shown by the solid bar with gradient R. Lines with gradients R}_0 \]

\[ \text{and R}_0' \] are also regression lines explained in the text.

Before (Vb1) and after (Vb2) the voltage-current response. The deviation is due essentially to variations in the natural telluric potentials discussed earlier. The best estimate of the resistance R0' to be substituted in Equation (1) when the decay is small is given by

\[ R_0' = R_0 - \frac{V b}{I}. \]
RESULTS AND INTERPRETATION

The apparent resistivity profiles have been interpreted using a BASIC computer program developed by Dr P Jackson (personal communication) based on Ghosh’s convolution method for VES [Ghosh 1971]. The program synthesizes an apparent resistivity profile for an n-layered model in which the variables are layer thickness and resistivity. Model profiles were compared with the field data and adjustments to the layering and resistivity values were made by trial and error to obtain as near correspondence as possible to the field data. However, in cases where there are very good conductors, such as sea-water, underlying a relatively resistive layer, such as an ice shelf, Ghosh’s method can produce inaccurate results because the Ghosh filter has too few coefficients to track a rapidly falling resistivity curve (Anderson 1979, Haines and Campbell 1980). Haines and Campbell (1980) have found that Ghosh’s method produces spurious apparent resistivity curves if the conducting layer \( \phi_2 \) has a resistivity less than around 1/20 that of the overlying medium \( \phi_1 \). i.e. a reflection coefficient \( K \) such that \(-0.05K<0.9\), where

\[
K = (\phi_2 - \phi_1)/(\phi_2 + \phi_1).
\]

The jump in resistivity between two layers where \( K < 0.9 \) can be smoothed by introducing a series of thin layers of intermediate resistivity wherever each layer has a higher reflection coefficient. To check the validity of this, three apparent resistivity profiles were compared. Two were obtained using Ghosh’s method, one being an ice shelf directly over sea-water and the other the same model subject to the addition of a relatively resistive layer, such as an ice shelf, beneath the ice shelf.

The third was obtained from an exact expression for apparent resistivity for a two-layer case (Telford 1982). The computed profiles at large separations deviate significantly from the field curves only when the water resistivity exceeds about 1000 ohm m, a value typical of low-salinity brackish water.

Estimates of the thickness of the ice shelf obtained in 1976 and 1977 by sledgeborne radio echosounding (RES) were 336\pm10 m for RJ 1 and 363\pm10 m for RK 2 (A H W Woodruff personal communication). Initially ice thicknesses were determined solely from the interpretation of the apparent resistivity profiles (Fig. 4) and were estimated to be 330\pm10 m and 370\pm10 m respectively, for the two sites. It is reassuring that the VES models do yield ice thicknesses within 5% of those obtained by RES. As the RES ice thicknesses are useful independent and accurate data, they have been incorporated as known parameters in all subsequent electrical resistivity modelling.

Figure 4 shows that for \( a<100 \) m the absolute value of resistivity differs between the two profiles at each site. This difference is related primarily to surface conditions along the line of each array. For example, the ice-shelf surface was wetter for profile RK 2-2, when pockets and pools of melt water were present within 1 m of the surface and much of the firm was saturated, than for RK 2-1. Profile RJ 1-3 was completed by mid-January 1980 while the surface was still comparatively dry. By the end of January 1980 melt was becoming more of a problem. For example, along the northern half of the RJ 1-4 array, some of the electrodes had penetrated through several alternate bands of solid ice and firm, through an air gap several tens of millimetres wide and into a pond of water 150 mm deep between two solid ice layers. The effects of free water (resistivity 1.5 to 5 kohm m, as determined using a conductivity bridge) reduce the gross resistivity of permeable surface layers. In addition, seasonal and diurnal temperature fluctuations should affect the resistivity of surface layers. Whether or not a resistivity-temperature dependence exists for bulk ice at a temperature
greater than -10°C remains an open question; however the surface resistivity of ice decreases as the melting point is approached (Maeno and Nishimura 1978). Some of the decrease in resistivity between profiles at the same site can be explained by a slight refreeze at the surface during the summer.

One of the aims of this work was to determine the extent to which the free water that forms on the surface of George VI Ice Shelf in summer and is subsequently refrozen affects the electrical properties of ice in a percolation-soaked zone. This has been discussed in part by Reynolds and Paren (1980). The electrical results indicate that refrozen free water affects resistivity only indirectly. The true resistivities at two sites on George VI Ice Shelf (4 and one on Ross Ice Shelf have been compared at depths of 10 m ($p_{10}$) and 100 m ($p_{100}$). At station BC on the Ross Ice Shelf, the ice-shelf density does not reach 0.9 Mg m$^{-3}$ until a depth of about 50 m (Bentley 1977) and densification is primarily by compaction. Resistivity decreases between 10 and 100 m such that $p_{10}/p_{100}$ equals about 8 (Bentley 1977). At RJ1 and RK2 there is a considerable range of densities with the top 10 m from 0.93 to 0.97 (Bishop and Walton 1981). At RJ1 there is a higher proportion of firm to ice than at RK2. Some compaction of firm layers occurs but densification is dominated by percolation and refreezing of melt water, so that $p_{10}/p_{100}$ is 3. At RK2 the firn is soaked during the summer months and densification is almost exclusively by refreezing of melt water; $p_{10}/p_{100}$ is then equal only to about 1.4. The ratio of resistivity ($p_{10}/p_{100}$) is thus an indication of the variation of density with depth. A large resistivity ratio implies low surface densities. A small resistivity ratio suggests a narrow range of density and that densification is affected by the percolation and refreezing of melt water.

For George VI Ice Shelf the resistivities obtained for ice at 100 m depth are within 4% of 48 kohm m; a steady-state temperature analysis such that $p_{10}/p_{100}$ equals about 8 (Bentley 1977). The difference at larger spacings probably has another explanation. A similar phenomenon has been reported by Bentley (1977, 1979) for half-spacings >30 m for two sets of resistivity profiles on the Ross Ice Shelf, where he found a difference of 12%. The effect is probably physically significant but one can do no more than speculate as to its cause. Bentley (1977) discounted preferred c-axis orientation as being responsible and suggested that a conductivity anomaly at a few metres depth could perhaps be produced by a healed crevasse. Buried crevasses transverse to the ice flow which may have incorporated snow could provide the necessary higher resistance barrier.

Computed apparent resistivity profiles which do not take into account any variation of resistivity with temperature provide the best fit to the field data. For this reason I believe that the resistivity of solid ice at a temperature greater than -10°C is independent of temperature. Nevertheless, in the modelling technique, the effect of temperature on resistivity has been considered. Assuming that the ice shelf is in steady-state with a lateral temperature gradient the analysis of Crary (1961) has been used to obtain a temperature profile through the ice shelf. From equation 3 of Crary (1961), the ice-shelf temperature gradient is proportional to

$$\exp \left[ \frac{\Delta h}{\alpha} \left( \frac{h}{2H} \right) \left( \frac{m}{a} - 1 \right) + 1 \right],$$

where $\alpha$ is the surface accumulation rate, $m$ the basal melting rate, $H$ the depth, $H$ the ice-shelf thickness, and $\Delta h$ the thermal diffusivity of ice. It is further assumed that resistivity $\rho$ is related to temperature by the Arrhenius function

$$\rho = \exp \left( \frac{E}{kT} \right),$$

where $E$ is the activation energy (eV), $k$ is Boltzmann's constant $8.62 \times 10^{-5}$ eV K$^{-1}$, and $T$ the absolute temperature (K). From these assumptions it is possible to obtain for each site a true-resistivity profile. Realistic values were assigned for the surface and basal ice-shelf temperature, thermal diffusivity, and accumulation rate. Dominant parameters were found to be the activation energy $E$, the Arrhenius equation and basal melting rate $m$. The coldest part of an ice shelf in steady-state with no lateral temperature gradients is the surface; on George VI Ice Shelf, the mean annual temperature is between -7°C and -10°C (Reynolds 1981) and the base is at the freezing temperature of sea-water, -2°C. For such a temperature regime, and with resistivities determined by the modelling techniques, an interpretation having a zero activation energy would be consistent with the findings of Camplin and others (1978). Nevertheless, models with an activation energy of 0.15 eV have been used; the fit to field data improved with
Increasing basal melting rate \( m_b \), and estimates were obtained for minimum bottom melt rate \( m_b \) \( (\text{Fig.5}) \). The minimum basal melting rate still compatible with field data was \( m_b = 0.15 \text{ m a}^{-1} \) for RK2-1. Shabtaie (personal communication) has used a computer model developed by Bentley (1977) to analyse the data from RK2. He assumed an activation energy of 0.25 eV, and obtained a basal melt rate of 1 m a\(^{-1}\).

On the remaining two profiles (RK2-2 and RJ1-3) best fits were obtained only if a layer electrically equivalent to a 5 m thick band of higher resistivity (250 to 300 kohm m) was included at the base of the ice shelf. This layer is not considered to have any physical significance for three main reasons. First, such a layer is not present on both profiles at each site. Second, the data at large electrode half-spacings for RK2-2 and RJ1-3 are not thought to be as reliable as data at equivalent spacings on the other two profiles (RK2-1 and RJ1-4). Third, a high resistivity layer at the base of George VI Ice Shelf is difficult to explain glaciologically. Similar high-resistivity basal ice layers have been suggested for various sites on the Ross Ice Shelf (Shabtaie and Bentley 1979) and Dome C (Thyssen and Shabtaie 1980). If it is therefore plausible that this basal ice, dating to the Wisconsin (Thomas 1976, Lennon and others 1979) which is a period climatically distinct from the Holocene, has different electrical properties. But on Palmer Land where the ice is significantly thinner, it is inconceivable that sufficient Wisconsin basins exist to provide a similar explanation. There is independent evidence for a basal melt rate for George VI Ice Shelf of the order of 2 m a\(^{-1}\) (Bishop and Walton 1981, Lennon and others 1982). This requires the ice at the base of the ice shelf at rosettes Juliet, which has been aloft for 175\( \pm 10\) a (based on data from Bishop and Walton 1981) to have been within 150 m or so of the surface of the ice at the grounding line, i.e. 70% of the ice column has been melted away. There is no known glaciological mechanism able to compress the whole of the Holocene ice column into 100 m at the grounding line of Goodenough Glacier.

CONCLUSIONS

The gross resistivity of shallow permeable layers tends to be reduced by warm, wet surface conditions. The ratio of resistivities at depths of 10 and 100 m is an indicator of the variation of density with depth; a ratio of 8 is typical of an ice shelf (e.g. Ross Ice Shelf) where compaction is the main mechanism of densification, while a smaller ratio (such as 2 found at rosettes Juliet and Kilo on George VI Ice Shelf) suggests that densification is influenced by percolation and refreezing of melt water. The bulk of the ice shelf, which lies within 5° to 8° of its sea-water melting temperature, behaves as if it has either no resistivity-temperature dependence in this temperature range or a slight dependence (activation energy of 0.15 eV) requiring a minimum basal melting rate of 1 to 2 m a\(^{-1}\). Such a rate is consistent with oceanographic measurements made at the northern ice front (Lennon and others 1982) and with independent theoretical estimates from surface measurements (Bishop and Walton 1981). The resistivities of the Ice at 100 m depth on George VI Ice Shelf differ by less than 10% from those at the same depth at station BC on the Ross Ice Shelf if an activation energy of 0.15 eV is assumed. This indicates that polar ice has a very narrow range of resistivity irrespective of the controlling densification mechanism. Selvick (personal communication) has investigated basal resistivities of George VI Ice Shelf from seismic refraction surveys made in 1979-80, and obtained: apparent resistivity profiles are consistent with there being sea-water of oceanic salinity under the ice shelf.

ACKNOWLEDGEMENTS

I am grateful to Dr P Jackson for providing the BASIC computer program, and to Dr C Bentley and S Shabtaie for useful comments. This paper has benefited greatly from discussions with Dr J B Paren.

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