Analysis of satellite-altimeter height measurements above continental ice sheets

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ABSTRACT. In order to estimate the accuracy of altimetric height measurements over ice sheets, an altimeter wave-form simulator has been developed, and different tracking methods have been tested. A large range of surface features, including large-scale and medium-scale features and micro-roughness have been taken into account for modeling of either surface- or volume-scattering. A large set of parameters affects the trailing edge of the radar wave form, so that re-tracking algorithms based on the detection of its leading edge provide better retrievals of the surface height than those based on the analysis of the whole wave form. A volume component is clearly present in the radar wave forms; its effect on the leading edge depends mostly on the snow grain-size (and therefore on the snow temperature) and on the pointing angle. However, on average, the induced error on the snow-surface height estimation should only be around 25 cm.

I. INTRODUCTION

Although satellite-altimeter radars were initially devised for operating over the ocean, potentialities of this instrument in the study of continental ice sheets were demonstrated very early (Brooks and others, 1978; Zwally and others, 1983).

Estimation of the mass balance of polar ice sheets or modeling of ice-sheet flow require an accuracy of the order of 10 cm in the measurement of ice-surface elevation. Remy and others (1989) have shown that the precision of the topography derived from a satellite-altimeter radar over the Antarctic ice sheet may be at the present time around 0.5-3 m and also shown how the associated error maps can be derived, on the condition that the initial measurement-error budget is known.

In addition to the well-known limits of altimeter radars over open water, other errors are specific to continental ice sheets, such as the surface-slope error (Brenner and others, 1983) or the inadequate tracking algorithms. Indeed, in contrast to the ocean, ice sheets present surface slopes of the order of 1°. In addition, radar-echo wave forms are affected by large-scale undulations (Martin and others, 1983) and by medium-scale features (snow dunes or sastrugi), so that the echo modeling is not as simple as for the ocean. Moreover, Ridley and Partington (1988) and Partington and others (1989) have suggested that the altimeter return is also influenced by volume-scattering. Because of this effect, the estimated elevation measured by the radar altimeter is lower than the actual surface. Furthermore, as volume-scattering depends on snow-grain characteristics, it may not be constant with time. This may seriously affect the potential of satellite altimeters to monitor ice-sheet surface elevations.

As many parameters affect the radar wave forms (Rapley and others, 1983; Ridley and Partington, 1988; Guzkowska and others, 1990), it is difficult to analyse the relative importance of their effects both because of the insufficient understanding of the physics of the scattering and because of the lack of values for these parameters.

Up to now, most altimetric wave-form simulators over ice sheets did not take into account volume-scattering, while modelling the latter has been achieved analytically (Partington and Rapley, 1986; Ridley and Partington, 1988; Partington and others, 1989). Here, we attempt to model volume- and surface-scattering simultaneously by adapting an altimeter wave-form simulator developed for a planetary radar (Thouvenot, 1990). Because the effect of the different snow parameters on the altimetric-height precision depends on the applied re-tracking technique, the existing techniques will be compared to estimate possible biases on the surface-height measurement due to volume-scattering. In this paper, we will focus the study on an area of Antarctica where the altitude is greater than 1000 m, because near the coast, other errors may lead to
poor accuracy. Thus, the surface characteristics (undulations) or volume characteristics (temperature and snow conditions) are selected as appropriate for such high altitudes.

The first section of the paper deals with the simulation of the surface effect, using an ice-sheet surface model. The paper continues with the simulation of the volume effect, and finally with its impact on the accuracy of the altimetric measurement.

II. PRINCIPLES OF WAVE-FORM SIMULATION

The altimeter wave-form simulator is based on two basic elements: the radar and the studied body, in this case the ice sheets.

The altimeter emits radar pulses at a pulse-rate frequency (PRF) of 1000–4000 Hz and records the reflected energy after its interaction with the illuminated area. Only a sample of each pulse echo is recorded in the radar-receiving window. One can consider the returned wave form of the radar pulse as the cumulative histogram of the energy returned from each illuminated surface point, sampled by a series of gates in the receiving window. For the Seasat altimeter, each of the 60 gates measured the energy return during a time, \( \tau \), of 3.125 ns. The instantaneous power (without thermal noise) received at time \( t \) from an illuminated point has been given by MacArthur (1978) as:

\[
P(t) = \frac{P_e}{L} \frac{\lambda^2}{(4\pi)^3} BT \int_{t}^{t+\tau} G^2 \sigma_0/d^4 \, dS \, \delta(\tau - 2d/c) \tag{1}
\]

where \( t \) is the arrival time of each illuminated point, \( d \) is the distance between the satellite and the aimed point, \( \tau \) is a 3.125 ns gate, \( \sigma_0 \) is the back-scatter coefficient, \( dS \) is a physical surface element, \( G \) is the real antenna gain, \( B \) is the band width, \( T \) is the pulse width (3.2 μs), \( L \) is the propagation losses, \( \lambda \) is the radar wavelength and \( P_e \) is its emitted power; \( c \) is the speed of light. The contribution of each physical surface element is therefore characterized by the time \( t \) of arrival, which depends on its position in the illuminated area and on the surface topography, and by its back-scatter coefficient \( \sigma_0 \).

The wave form of the radar echo from a flat surface can be separated into two parts. Its leading edge is caused by the initial interaction of the pulse with an expanding quasi-circular area, the maximum width of which is affected by the radar-pulse length and the medium-scale features such as sastrugi. At its maximum width, this area is known as the pulse-limited footprint. After this initial stage, the illuminated surface becomes an annulus of progressively increasing radius and approximately constant surface area. The reflected energy from this annulus is attenuated by the antenna pattern and forms the trailing edge of the wave form.

Considering the availability of Seasat data over Antarctica and the desire to make comparative tests, we modeled the altimeter simulator on the description of the Seasat altimeter (MacArthur, 1978). This altimeter operated at a frequency of 13.6 GHz (\( \lambda = 2.3 \) cm), where the echo is mostly sensitive to surface features. Indeed, at this frequency, the volume echo, due to back-scatter of the radar signal from below the snow surface, is not dominant (see below). The transmitted pulse has a band width \( B = 320 \) MHz. The antenna is a 1 m parabolic dish. Over a flat surface, the diameter of the beam-limited illuminated surface depends on the 3 dB two-way antenna beam width defined in degrees as:

\[
\delta = 70\lambda/D
\tag{2}
\]

where \( \lambda \) is in cm and \( D \), the parabolic dish diameter, is in meters.

The software simulator generates return wave forms for different off-nadir pointing angles (Fig. 1) from different simulated surfaces. One can schematically describe the software in three successive parts: first, the spacecraft configuration includes effects of the elevation and geographic location of the satellite, and of the off-nadir pointing angle. Secondly, the pulse-limited footprint is determined according to its location in the beam-limited footprint, taking account of surface slope and roughness. The width of the acquisition window, within which the return energy is recorded, has been set at 40 m, as a compromise between computed execution time and compatibility with surface roughness. This leads to considering 6 x 10^5 points in the illuminated area. Thirdly, the different characteristics of the surface- or volume-scattering are then easily taken into account according to their statistical distribution, using a Monte Carlo technique.

Finally, the temporal evolution of the echo is calculated by summing the responses of all points from the illuminated surface, at their corresponding arrival times.
III. MODELING SURFACE FEATURES

The topography of ice sheets, and more especially of Antarctica, can be described by four main kinds of relief: two on a large scale—the near-parabolic profile and undulations—both related to the ice flow above the bedrock (McIntyre and Drewry, 1984), and two on medium to small scales—sastrugi and micro-roughness—created by winds (Kobayashi, 1979). The smaller-scale features, micro-roughness, affect the back-scatter coefficient. The other scales affect the back-scatter coefficient and/or the arrival time.

Micro-roughness is taken into account in either one of two models of back-scattering, one with a Gaussian distribution of slopes and the other with an exponential distribution (Fung and Eom, 1983). As an example, the former is described by:

\[ \sigma_0 = \frac{R^2}{2s^2 \cos^4 I} \exp\left(-\frac{\tan^2 I}{2s^2}\right) \]

where \( s^2 \) is the r.m.s. surface slope, \( I \) is the incidence angle (see Fig. 1) and \( R \) is the Fresnel coefficient taken at the vertical and given by:

\[ R = \left(\frac{1 - \sqrt{\varepsilon}}{1 + \sqrt{\varepsilon}}\right) \]

where \( \varepsilon \), the dielectric constant, is linked to the snow density (Tiuri and others, 1984). This back-scatter model is adapted from that for the oceanic surface. No in-situ data are available to verify its validity. However, from this model, the echo decreases rapidly from about 5 dB at the vertical to -5 dB at 20° incidence, as is observed by the Seasat scatterometer data (Ledroit and others, 1993), which operated at the same frequency as the altimeter.

Sastrugi are from centimeters to about 1 m in height and up to 10 m in wavelength (McIntyre and Drewry, 1984). These features are elongated in the katabatic upwind direction and are disymmetric with one side steeper than the other. In the simulation, only energy reflected from the gently sloping side is taken into account, considering that the return power from the other side is insignificant in comparison. Thus, sastrugi are modeled by three points of elevation taken randomly for each illuminated point (Fig. 1).

Large-scale undulations are dome-shaped with heights of the order of meters to tens of meters and wavelengths of kilometers to tens of kilometers (Fig. 2b). They affect the radar wave forms because the corresponding curvature of the surface varies on the same scale as the illuminated area (Martin and others, 1983). In the altimeter simulator, the elevation connected to this modeled relief is estimated at each point in the illuminated surface by a two-dimensional sine function.

As shown in Figure 2a, a near-parabolic surface fits the large-scale ice-sheet topography over a few hundred kilometers. In an altimetric measurement, the diameter of the beam-limited footprint is 20 km to 30 km, and the pulse-limited footprint is considerably smaller, so that the parabolic relief can be approximated as a plane. In the software, we modeled this as equivalent to an off-nadir pointing angle. Indeed, the same wave form can be created by two different configurations (see Fig. 3) by an off-nadir pointing angle or by a surface slope. Note that the altimetric height relates to the distance of the nearest point from the satellite, which is shifted from the nadir \( N \). This effect is called the slope-induced error and can be corrected at a later stage, during data processing (Brenner and others, 1983; Remy and others, 1989).

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Fig. 2. Seasat altimetric profile above the Antarctic ice sheet fitted by a parabolic function (a) and its residual height showing undulations (b). From Remy and others (1989).

Fig. 3. Geometry for the large-scale slope effect. The large-scale topographic features (a) are taken into account as an off-nadir pointing angle (\( \beta \) in Fig. 1) of the same value (b).
Fig. 4a-c. Simulated wave forms using Seasat values for the different radar parameters. Pointing angle, sastrugi r.m.s., half-amplitude and wavelength of the undulations are indicated on the righthand side. The point of sight is on the top of an undulation (T), on its edge (E), or on its bottom (B). The main difference between Figure 4a and b is the value of the pointing angle. Figure 4c shows the impact of the undulation characteristics.

IV. TESTS WITH TRACKING ALGORITHMS OVER SIMULATED SURFACES

Figure 4a-c shows examples of simulated wave forms. The simulated relief parameters are indicated on the right-hand side of the figure (pointing angle, r.m.s. of the sastrugi, amplitude and wavelength of undulations). The "amplitude" means half the peak-to-trough height difference. A data bank of over 60 different surface-echo wave forms was created by varying the set of parameters.

To derive a measurement of the surface elevation, the altimeter records the power in the series of gates for each pulse echo. In order to center the return wave form within the acquisition window, the altimetric height is followed on board through a "height-tracking loop", which anticipates the arrival time of the echo from that of
The location of the half-power point is then formed by the following equation:

\[ A = \frac{1}{2} \sum_{n=-30}^{+30} \frac{P_n^2}{\sum_{n=-30}^{+30} P_n}, \]  

(7)

with \( P_n \) the power of each gate sample (\( n \), numbered from -30 to +30) in the receiving window. \( W \), the wave-form width, is then obtained by the relation \( 2AW = \Sigma P_n \), with the result:

\[ n - W = \frac{\left( \sum_{n=-30}^{+30} P_n \right)^2}{\sum_{n=-30}^{+30} (P_n)^2}. \]  

(8)

The location of the half-power point is then formed by the following equation:

\[ P(p) = P_{\text{max}} \cdot \left(1 + \text{erf}(\chi(p - p_0))/2, \right) \]

where

\[ (1 + \text{erf}(x))/2 = \pi^{-1} \int_{-\infty}^{x} \exp(-u^2) \, du. \]

(6)

\( \chi \) is an adjustable parameter which describes the slope of the error-function \( \text{erf} \): the larger \( \chi \), the steeper the slope. \( p_0 \) is the position of the half-power point to estimate. \( P_{\text{max}} \) is the larger power value in the receiving window. In fact, the method consists in defining and adjusting a window around \( p_0 \) by least-squares regression.

A second algorithm is the Offset Center of Gravity method (OCOG), a full wave-form re-tracker developed by Wingham and others (1986) for ERS-1 data. Note that this method was not initially designed to achieve this task (personal communication from D.J. Wingham). This method is based on the definition of two wave-form shape parameters, its "amplitude", \( A \), and its "width" \( W \). The wave-form amplitude is described as a function of time, or equivalently gate \( p \):
Type 2. "Flat trailing-edge echoes" pattern.

Type 3. "Specular echoes" pattern.

These three types are also encountered in actual measurements, the last one being mostly encountered when the wave impact is on the edge of undulations (see Fig. 4). We generated height errors, i.e. shifts of the wave form in the receiving window. These shifts ranged from -20 to 20 range bins, each bin corresponding to about 50 cm and thus to one gate. The re-tracking error is then defined as the difference between the actual shift and the values derived from the re-tracking algorithms. Figure 6 compares, for the three types, the height error estimated by the three re-tracking algorithms with the actual shifts: the latter are plotted in range bins on the X-axis and the height error, also measured in range bins, on the Y-axis. A negative value corresponds to a late echo in the receiving window. Each diagram also indicates the r.m.s. of the difference between the actual and retrieved values, also expressed in range bins.

The “fitting process” has the best responses, for all three types, for positive shifts as well as for negative ones. The OCOG method has a linear behavior for both positive and negative shifts. The scatter and the re-tracking error are both worse for specular wave forms. The GRGS method has unacceptable responses for very large shifts, most particularly for very early echoes of the first type. Indeed, this re-tracking algorithm should be sensitive to the power of the trailing edge (see Remy and others, 1990), which is largest for the first type of wave form. However, the r.m.s. is good for specular wave forms.

The fitting process, a leading-edge re-tracker, is thus the best method for obtaining a precise estimation of the range to the pulse-limited footprint. Indeed, undulations and off-nadir pointing affect the shape of the wave form and more especially its trailing edge, so that the different full wave-form re-trackers are sensitive to effects (surface slope, off-nadir pointing angle, ...) other than the height in the beam-limited footprint.

V. VOLUME ECHO

Ridley and Partington (1988) and Partington and others (1989) suggested that both volume- and surface-scatter-
ing affect the altimeter-radar echo to variable extents and that the error due to radar penetration of the snow is between 0 and 2–3 m. On the other hand, empirical studies (Remy and others, 1990; Remy and Minster, 1991; Ledroit and others, 1993) suggest that the altimeter returns over dry snow are dominated by surface-scattering. Thus, in order to estimate this signal “pollution”, we add volume-scattering to the simulation of echo wave forms.

If one neglects internal-layering effects, the snow cover of the ice sheets may be described by an aggregate of snow grains governed by their mode of deposition and their further consolidation. It may be simplified as a randomly stratified medium with layers of varying density, comprising grains that are more or less spherical and of various sizes, and where compaction increases with depth. The back-scatter coefficient due to volume-scattering is then given (Thouvenot, 1990) by:

\[ \sigma_v = \frac{(\pi r^2/\chi^2)}{\left[ \sum_{i=1,0}^{\infty} (-1)^i (2i+1)(a_i - b_i) \right]^2} \]  (14)

where \( \chi = k_0 r \), \( k_0 \) being the radar wave number in empty space, and \( (a_i) \) and \( (b_i) \) are two series of coefficients (Thouvenot, 1990).

The attenuation of each layer is given by:

\[ \tau = \exp[-2\sqrt{3\tau/\rho \cos \theta_0}] \]  (15)

where \( \delta_p \) is the penetration depth, equivalent to \( 1/k_b \) (\( k_b \) being the extinction coefficient, which is the sum of the absorption coefficient, \( k_a \), and of the scattering coefficient, \( k_s \)), \( \theta_0 \) is the refraction angle given by the Fresnel law.

The impact of all the layers is obtained by summing the different powers \( \tau_a \) from the first to the last one, \( n_a \) being the number of layers. Of course, echoes from the first layer are not attenuated.

\[ \tau_{tot} = [1 - \tau_a(\tau_{a+1})]/(1 - \tau_a). \]  (16)

\( n_a(I) \), the number of spheres by layer is given by:

\[ n_a(I) = \frac{\text{seq}(I)}{3\pi r^2}. \]  (17)

\( \text{seq}(I) \) is the equivalent surface balanced by the decrease of the antenna gain.

For modeling of the volume-scatter, we kept the skeleton of the initial software, which allows addition of the volume-scatter to any surface. At the time of the initial impact of the radar pulse on the medium, the initial illuminated volume, and thus the contribution to the volume component, is small but increasing. This can have an affect on the width of the leading edge of the echo wave form, which plays a key role for re-tracking and thus for the precise retrieval of the altimetric height. So, because the column return power depends on the illuminated volume, we determined the exact involved volume according to the random sastrugi shapes.

However, we only considered simple scattering which overestimates the volume back-scatter compared to a multiple-scattering model.

The penetration depth of the pulse has been limited to about 9 m. According to Rott and others (1985), for a frequency of 13.5 GHz, the penetration depth is around 8 m. Since we are mostly concerned with the impact of the volume component on the leading edge of the wave form, this penetration depth is quite adequate.

VI. ANALYSIS OF RADAR WAVE FORMS WITH VOLUME ECHO

Figure 7 shows volume echoes modeled without any relief and with zero off-nadir pointing angle. Only the curvature of the Earth is taken into account. Three main parameters are considered: temperature, the average grain radius and density, which in Antarctica vary respectively from -15° to -40°C, from 0.5 to 1 mm and from 0.35 to 0.45 Mg m^-3. These values are representative of in-situ measurements (Paterson, 1981). The average radius of snow grains is the most sensitive parameter in our model of volume-scattering. The upper value of 2.5 E-12 W from our model is an upper bound of volume echo: it remains lower than thermal noise (3.9 E-12 W for Seasat). The volume-echo component is therefore a priori low.

A separate bank of 20 surface- and volume-echo wave forms has been created by combining the various parameters for the two processes. Figure 8 compares, for the three types of echo, wave forms with the surface component only (full line) with wave forms where the volume component is added (dashed line). The same parameters for the volume echo have been selected in each of the three cases. It can be seen that the volume component mostly affects the trailing edge. This effect decreases with increasing off-nadir pointing angles. The volume component contributes to 15–20% of the total

Fig. 7. Volume echoes modeled for different values of the parameters, snow density, grain radius and snow temperature.
wave-form power, depending on the surface roughness and on the pointing angle.

The radius of snow grains can evolve with time, because of compaction and aggregation phenomena, and can reach values larger than usual. Figure 9 shows the behavior of the volume-scattering power according to this parameter. Temperature and density have been fixed to respectively -40°C and 0.45 Mg m⁻³. It can be seen that, for large values of the grain radius, the curve reaches an asymptote, around -2.5 dB, which can be considered as an upper threshold for the volume component.

FIG. 8. EXAMPLES OF MODELED ECHOES WITH THE SURFACE COMPONENT ONLY (FULL LINE) AND THE VOLUME COMPONENT (DASHED LINE). NOTE THAT THE SURFACE COMPONENT IS SET TO ITS MINIMUM VALUE AND THAT THE APPARENT RATIO VOLUME/SURFACE IS THEN A MAXIMUM. TYPE 1 ECHO IS AN EXAMPLE OF AN ECHO FROM A STRONG OFF-NADIR POINTING ANGLE; TYPE 2 REPRESENTS A FLAT TRAILING-EDGE ECHO PATTERN, AND TYPE 3 IS A "SPECULAR ECHO" PATTERN. VALUES FOR SNOW DENSITY, GRAIN RADIUS AND SNOW TEMPERATURE ARE 0.45 Mgm⁻³, 1.00 mm, -40°C, RESPECTIVELY. THE VALUES OF SURFACE PARAMETERS ARE DIFFERENT FOR EACH MODELED ECHO. THE TYPE 3 MODELED ECHO ARRIVES IN ADVANCE BECAUSE THESE VALUES ARE VERY LARGE.

VII. INDUCED ERROR FROM THE VOLUME COMPONENT ON THE RE-TRACKING TECHNIQUE

We have shown that the volume component affects the wave-form shape and more especially its trailing edge. It is therefore a priori expected that a leading-edge re-tracker will be more adequate for estimating the surface height.

We have estimated the influence of the volume echo on the surface-height determination using the three re-tracking methods. Table I gives the average effect and its standard deviation for the whole bank of 20 wave forms. It is always lower than half a gate. This effect has to be added to the initial re-tracking error due to the surface echo. As previously seen, the different re-tracking methods always define an elevation lower than the real one (Fig. 5). The volume component also induces an error in the same direction (Table 1). At first sight, the most adequate re-tracking method remains the fitting process developed by Martin and others (1983). For the same reason as previously, the dispersion in the OCOG method is close to half a gate.

Table 1. Average influence and its standard deviation of the volume echo on the surface-height retrieval for the three different re-tracking algorithms, fitting process, OCOG and GRGS. These values have been calculated using a bank of 20 simulated wave forms with different values of the parameters (see text). They are expressed in gate numbers and in centimeters

<table>
<thead>
<tr>
<th>Re-tracking methods</th>
<th>Volume error</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Gates cm</td>
</tr>
<tr>
<td>Fitting process</td>
<td>-0.39 ± 0.44 -18 ± 21</td>
</tr>
<tr>
<td>OCOG</td>
<td>-0.49 ± 0.51 -23 ± 24</td>
</tr>
<tr>
<td>GRGS</td>
<td>-0.32 ± 0.34 -15 ± 16</td>
</tr>
</tbody>
</table>

In Figure 10, the volume effect induced by the different methods is plotted against the volume/surface ratio. Contrary to intuition, larger errors are induced by lower ratios. Indeed, as can be seen in Figure 7, for large volume echoes, the leading edge is straighter and closer to the middle of the receiving window. Thus, when volume-scattering is important, the estimation of the middle of the leading edge of the wave form and hence the retrieval of the height are not affected too much. Note also that full wave-form re-tracking techniques, in particular the GRGS algorithm, are less sensitive to this volume/surface ratio, because they take into account the whole signal.

On the other hand, the result depends on the off-nadir pointing angle. The greatest errors are induced by the higher off-nadir angles even if the volume/surface ratio is low. As a matter of fact, for large off-nadir pointing angles, the wave-form shape is strongly dependent on the

FIG. 9. BEHAVIOR OF THE VOLUME BACK-SCATTER COEFFICIENT AS A FUNCTION OF THE SNOW-GRAIN RADIUS, FOR SNOW TEMPERATURE OF -40°C AND DENSITY OF 0.45 Mg m⁻³.
the width and slope of the leading edge of the surface component is almost vertical. Then, the width and slope of the leading edge practically remain insensitive to the volume effect. In this case, the total error during re-tracking is very low, whatever the re-tracking technique.

VIII. CONCLUSION

We have analyzed the accuracy of the various techniques of satellite-altimeter echo analysis for determining the elevation of continental ice sheets.

The echo wave forms are mostly affected by surface effects, in particular, the off-nadir pointing angle—or equivalently by the surface slope—and by the surface roughness. The modeled power return due to volume back-scatter by the snow cover does not exceed $-2.5 \text{ dB}$ for acceptable values of snow grain-size, temperature and density, and affects mostly the trailing edge of the echo wave form. Thus, for all existing algorithms used to estimate the surface height from the echo wave form, the error due to volume back-scatter is lower than $50 \text{ cm}$. However, both surface and volume effects are less significant on the leading edge of the wave form so that algorithms that use a model function to search for the middle of this leading edge are more appropriate to determine the altimetric surface height. In particular, the method proposed by Martin and others (1983) presents biases lower than $2 \pm 2 \text{ cm}$ due to surface effects and of the order of $-20 \pm 20 \text{ cm}$ due to volume effects. We strongly recommend that such a method be applied to the ERS-I data, as proposed by the group of ice-sheet investigations approved by ESA to receive the altimetric data (personal communication from R. Thomas).

In addition to surface elevation, as well as the back-scatter coefficient (Remy and others, 1990), the extraction of other parameters from altimeter-radar wave forms is difficult because of the large number of unknown antenna gain. The return is characterized by a long, attenuated leading edge. Although the volume echo is small in this case, its effect on height retrieval is large, because it affects the end of the leading edge, which is already hazy. Note that the pure surface re-tracking error is also greater for type 1 wave forms (see Fig. 6). On the other hand, for low off-nadir pointing angles, the leading edge of the surface component is almost vertical. Then,
parameters. Figure 11 shows two wave forms simulated with totally different surface and volume parameters, but which are quite similar whether on their leading or on their trailing edges. The power integrals are also almost equivalent. Estimating geophysical parameters (snow grain-size, surface roughness) from the radar echo are then strongly under-determined. In particular, estimation of the volume component from the wave form would be difficult. The altimetric height error due to this component cannot be derived from the re-tracking method. A height bias of the order of $20 \pm 20$ cm could always be present due to this effect.

One of the altimetric parameters that could have a strong effect on the volume echo is the radar frequency. Figure 12 shows a wave form with constant snow-parameter values, for different radar frequencies. For frequencies higher than 13.5 GHz, the scattering volume is increased by radar-penetration depth decreases. The leading edge of the wave form is therefore narrower and the signal comes mainly from the upper layers. In that case, the accuracy of the surface elevation should probably be better. Conversely, using two-frequency altimeters could help in separating the various effects.

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The accuracy of references in the text and in this list is the responsibility of the authors, to whom queries should be addressed.