A surge of North Gasherbrum Glacier, Karakoram, China

Christoph MAYER, 1 Andrew C. FOWLER, 2 Astrid LAMCRECHT, 3 Kilian SCHARRER 4

1 Commission for Glaciology, Bavarian Academy of Sciences, Allons-Goppel-Strasse 11, D-80539 Munich, Germany
E-mail: christoph.mayer@lrz.badw-muenchen.de
2 MACSI, Department of Mathematics and Statistics, University of Limerick, Limerick, Republic of Ireland
3 Institute of Meteorology and Geophysics, University of Innsbruck, Innrain 52, A-6020 Innsbruck, Austria
4 School of the Environment and Society, Swansea University, Singleton Park, Swansea SA2 8PP, UK

ABSTRACT. Between 2003 and 2007, North Gasherbrum Glacier on the northeastern slope of the Karakoram mountains in Asia underwent a dramatic acceleration, during which a velocity wave propagated down the glacier. There was a significant transfer of ice from up-glacier downstream, which resulted in a strong surface elevation increase over the lower tongue, but only a moderate advance of the glacier snout. We interpret this behaviour as that of a glacier surge, and we explain the observations by means of a simple version of the Kamb drainage-switching theory.

INTRODUCTION

Surging glaciers occur in most mountain ranges of the world, but in the Karakoram a concentration of periodically fast-moving glaciers can be observed (Hewitt, 2007). About 37% of this extensive mountain range between the Hindu Kush in the west and the Himalaya in the south and east is covered with glaciers (Shroder and Bishop, 2010) and provides many of the largest glaciers outside the polar regions. In the centre, major glaciers, like Baltoro Glacier (∼64 km) and Siachen Glacier (∼72 km), drain from a small mountain region consisting of some of the highest mountains in the world, with four peaks higher than 8000 m a.s.l. Compared with the high elevations in the Himalaya, this region is dry, with almost desert-like valley floors. However, a strong precipitation gradient exists between the low parts of the valleys and the high mountain slopes, where the maximum precipitation is expected to occur between 5000 and 6000 m a.s.l. (Batura Glacier Investigation Group, 1979; Wake, 1989; Miehe and others, 2001) and reaches 2000 mm a 1. Most of the precipitation occurs during winter and spring, when westerly winds dominate the large-scale weather system. However, variations are large, and, depending on the strength of the monsoon, considerable precipitation amounts can also be accumulated at high elevations during summer (Wake, 1989). Since the 1960s a positive change has been observed for annual precipitation, while winter precipitation seems to be declining, at least at some meteorological stations in the region (Archer and Fowler, 2004). The topography is characterized by extensive valley systems and large elevation gradients in the headwaters. Often the accumulation basins, which generally occupy the elevation band of maximum precipitation, are still towered over by mountain slopes 2000–3000 m high. Consequently, many of the glaciers are fed, to a considerable extent, by avalanche snow (Hewitt, 1998; Mayer and others, 2006).

From 1978 onwards (with the construction of the Karakoram Highway) glacier research activities increased in the Karakoram, starting with the Chinese Batura Glacier Investigation Group (1979) and other projects like the Canadian Snow and Ice Hydrology project (e.g. Hewitt and Young, 1990). In more recent times these activities have also included remote-sensing studies, focusing on the glaciers in this region (e.g. Bishop and others, 2000; Osipova and Tsvetkov, 2002; Quincey and others, 2009). Today the overall glacier mass balance is thought to be negative (Shroder and Bishop, 2010), but a considerable number of advancing glaciers were observed during the 1990s (Hewitt, 2005). At the northeastern side of the Karakoram the conditions changed from warm/dry to warm/humid with a clear trend towards more negative mass balances in the early 1990s, estimated from river discharge measurements (Gao and others, 2010).

The glaciers in the Karakoram and in Alaska, USA, represent ∼90% of the known surging glaciers (Hewitt, 1969); in the Pamirs a large number of glaciers are potential surge-type glaciers, with >60 observed surge events (Kotlyakov and others, 1997). In the Karakoram >30 surges have been reported since the 1860s (Hewitt, 1998), and many more probably went unnoticed. During recent times it seems that surge activity has been increasing (Hewitt, 2007). Many of the reported surges in the Karakoram occur in tributaries of large glaciers, while the main glaciers show no signs of strong periodic advances. These tributaries are often steep, with an altitude range of >2000–3000 m within only 10–15 km (Hewitt, 2007). Most of these surge events last only a few months. Even for normal dynamic conditions, the surging glaciers in the Karakoram can be expected to provide a large mass transport from the accumulation basins, with high precipitation, into the drier, lower areas. Glacier length seems not to be an indicator for surge sensitivity, as the longest glaciers in the Karakoram are not known to surge, while most surging glaciers in this area are medium-sized glaciers with a large elevation range (Hewitt, 2007).

To date, glacier surges in the Karakoram have been observed either by repeated visits to the area and subsequent descriptions of the geometric changes of the glacier tongues and superficial moraines (Hewitt, 2007), or the investigation of photographs from different dates (Diolaiuti and others, 2003). No information exists at present concerning the temporal evolution of the dynamic state of a surging glacier in the Karakoram.

North Gasherbrum Glacier

The region of the highest mountains around Baltoro Glacier, including the second-highest peak in the world, K2, was visited by European travellers as early as the 19th century. Members of a large expedition mapped this glacier and
the surrounding mountains in detail in 1909 (De Filippi, 1912). In contrast, the eastern part of this mountain group is much less known. To the east of Concordia, the main junction of Baltoro Glacier, the Gasherbrum and Broad Peak group comprises about a dozen peaks, with three reaching >8000 m a.s.l. To the north and east of these massifs is the drainage basin of North Gasherbrum Glacier, while the southern part of the Gasherbrum group contributes to the much smaller South Gasherbrum Glacier, a tributary of Baltoro Glacier. North Gasherbrum Glacier is fed by avalanches originating from the peaks of Gasherbrum II (8035 m a.s.l.) and Gasherbrum IV (7925 m a.s.l.) in the south and Broad Peak (8047 m a.s.l.) in the west of the main accumulation basin (Fig. 1). The slopes of the mountain walls surrounding the high-accumulation basins are steeper than 40° in many cases. The glacier is ~23 km long, covers an area of ~67 km² and the glacier tongue is formed by four tributaries of different sizes. Besides the main trunk of the glacier, originating from a basin between Broad Peak, Gasherbrum IV and Gasherbrum II, only the lower, southern tributary seems to contribute a considerable amount of ice to the glacier. The accumulation basin of the main trunk is situated between 5400 and 6000 m a.s.l., with some parts reaching ~6600 m a.s.l. However, the very steep slopes around the accumulation basins probably provide a considerable part of the total accumulation as avalanches. Ice in the ablation area of the glacier is mainly flowing eastward and later northeastward from ~5000 m a.s.l. until the glacier terminus at 4230 m a.s.l. This part of the glacier is ~15 km long, which results in a mean surface gradient of 0.05. The entire glacier shows an elevation difference of >3800 m from the highest peak to the glacier tongue, and thus the mean slope is ~3° × the slope of the glacier tongue. Due to the high fraction of avalanche snow in the accumulation basins, originating from elevations above 6500 m, it can be expected that the glacier is rather cold above the ablation zone. Only the lower tongue receives a large amount of meltwater, which will shift this part of the glacier into temperate conditions.

During a short visit in 2006 the lower part of the tongue was visually investigated. The glacier tongue shows supraglacial debris cover of ~50%, which mainly originates from the confluence between the main trunk and a southern tributary 10 km from the snout, at ~4700 m elevation. The northern half of the tongue is only partly covered by debris, but shows an extremely rough surface, with a very high density of ice sails, sharp ice pinnacles rising from the glacier surface up to 15–20 m. There is no indication of large velocity gradients between the main trunk and the inflowing tributaries. On the eastward-flowing lower glacier tongue, no shear zones can be detected between the individual glacier parts, indicating that the main trunk dominates the dynamical conditions of this part of the glacier. The snout of the glacier ends in the Shaksam valley, a tributary of the Yarkand valley.

The Shaksam valley has an area of ~8200 km², of which 32% is covered by glaciers and perennial snowfields. The long-term equilibrium-line altitude (ELA) is situated between 5100 and 5400 m elevation (Feng, 1991). The main discharge from snow and glacier melt occurs between June and September, when 80% of the total discharge is generated. The snout position of North Gasherbrum Glacier is known to vary between ~500 m from the right valley wall (Feng, 1991) and touching the wall (Desio, 1930, 1955). The water from these rivers drains via the Yarkand River into the Tarim basin, one of the largest inland depressions in the world. As the distance between the glacier terminus and the opposite valley wall is just a few hundred metres, even minor advances of the glacier could block the Shaksam River and produce an ice-dammed lake. The glaciers in the upper Shaksam valley are known to produce glacier-dammed lakes. So far the damming of a lake by North Gasherbrum Glacier has not been not observed, but the upstream Kyagar and Tram Kangri Glaciers have a long history of destructive glacier lake outburst floods (Feng, 1991) which could affect almost two million people and widespread infrastructure downstream (Hewitt and Liu, 2010). Such outburst floods from lateral glaciers blocking the main valley occur in both the Indus and Yarkand basins (Feng and Liu, 1990), and >20 glaciers have been identified where this happened in the 20th century (Hewitt, 1982; Zhang, 1992).

North Gasherbrum Glacier is classified as a surge-type glacier by Kotlyakov (1997). But so far no surge has been observed and there has not been any clear sign of former surge activity. This is in contrast to its southeastern neighbour, Urdok Glacier, which shows a series of looped moraines, originating from its northern glacier branch, and clearly indicates at least five surge events of this tributary during the past. While investigating glacier changes in the central Karakoram on the basis of remote-sensing imagery, it was observed that North Gasherbrum Glacier showed non-typical surface displacements over a certain time period. This observation led to a more detailed analysis of the temporal evolution of surface changes on this glacier; the neighbouring glaciers did not show any anomalies in the same time period.

The region east of the highest peaks in the main ridge is bounded by the Karakoram fault, a major geologic feature running for >750 km from the Pamirs to the Kailash region (Searle and Phillips, 2007). North Gasherbrum Glacier flows across this fault, and the middle part of the tongue (~4500 m a.s.l.) is situated directly above the fault. In
Here maximum velocities during the surge in 1989 were exists for Medvezhiy glacier (Kotlyakov and others, 1997). type glaciers are identified, a very detailed observation 1900advance due, presumably, to declining mass balance throughout the world, although few have been studied in recent surges have been moderate. Surging glaciers occur (1998) on Bakaninbreen, Svalbard, both of whose most Trapridge Glacier, Yukon, Canada, and by Murray and others 2001–09. Landsat-7 provides Our analysis of the dynamic state of North Gasherbrum DATA AND IMAGE ANALYSIS information about the Landsat-7 ETM+ acquisitions, the Image A Image B Period Season Image pairs used and their periods 04/09/00 21/07/01 320 Annual 21/07/01 09/08/02 384 Annual 09/08/02 15/10/03 432 Annual 15/10/03 15/09/04 336 Annual 15/09/04 02/09/05 352 Annual 02/09/05 07/10/06 400 Annual 07/10/06 27/11/07 416 Annual 27/11/07 06/06/08 192 Winter 06/06/08 12/10/08 128 Summer 06/06/08 27/07/09 416 Annual 12/10/08 27/07/09 288 Annual 12/10/08 12/08/09 304 Annual 12/08/09 29/09/09 352 Annual 27/07/09 29/09/09 64 Summer 07/10/08 02/12/09 128 Summer/autumn 27/07/09 02/12/09 64 Summer 12/08/09 02/12/09 112 Autumn consequence the mountains in the accumulation zone of the glacier consist of Gasherbrum–Broad Peak quartz diorite, which intruded the limestones of the Shaksgam and Aghil formations. Thus the erosion rates in the higher regions can be expected to be low (Searle and Phillips, 2007), while the lower parts of the glacier might receive a considerable amount of debris from deformed limestone. Glacier surges Glacier surges are periodic advances of a glacier, often taking the form of rapid motion which leads to a sudden advance of the glacier snout. A typical example is Variegated Glacier, Alaska, whose advance in 1982–83 was well documented by Kamb and others (1985). Largely based on that work, the common perception of a surging glacier was that it always involved a rapid advance of the terminus, associated with high velocities. However, in their classic early survey, Meier and Post (1969) advised that surges came in all shapes and sizes, a fact subsequently borne out by the detailed observations of Frappé-Sénéclauze and Clarke (2007) on Trapridge Glacier, Yukon, Canada, and by Murray and others (1998) on Bakaninbreen, Svalbard, both of which most recent surges have been moderate. Surging glaciers occur throughout the world, although few have been studied in the Himalaya. In the European Alps, the last known surging glacier, Verragtferner, lost its oscillatory behaviour after its 1900 advance due, presumably, to declining mass balance warmed by warming since the 1800s (Höinkes, 1969). In the Pamirs, where a large number of potential surge-type glaciers are identified, a very detailed observation exists for Medvezhiy glacier (Kollyakov and others, 1997). Here maximum velocities during the surge in 1989 were observed to be 70 cm d$^{-1}$ ∼1 km upstream of the advancing glacier tongue. DATA AND IMAGE ANALYSIS Our analysis of the dynamic state of North Gasherbrum Glacier is based on Landsat-7 Enhanced Thematic Mapper Plus (ETM+) data from 2001–09. Landsat-7 provides multisolrfrtional images with different spatial resolutions, where the panchromatic band 8 provides the smallest pixel size of 15 m. Landsat-7 ETM+ data cover the period since 1999 and, due to a repeat coverage of 16 days, there is a good possibility of compiling multi-year time series of cloud-free imagery for a specific region. We used feature tracking (Scambos and others, 1992; Strozzi and others, 2002) on a collection of repeated Landsat-7 ETM+ imagery to measure seasonal and interannual ice-flow rates for the period 2001–09. This method aims to find similar patterns (e.g. groups of crevasses advecting down-glacier, or specific supraglacial debris patterns) between two consecutive images. The principles of this method are based on a cross-correlation algorithm used on image patches of repeat-pass satellite image pairs (Strozzi and others, 2002). The method relies on first matching non-moving features within the two consecutive images (such as rock outcrops), in order to find the geometric solution to co-register the image pair with subpixel accuracy. This was done by manually identifying tie points in the corresponding image pairs. To minimize any geometric distortions, only images of the same path/row were used in this study (path 148, row 35). North Gasherbrum Glacier is situated in the centre of this footprint, enabling us to use Landsat-7 ETM+ acquisitions, even after the scan-line correction failure in May 2003, providing full coverage over the entire glacier catchment (Fig. 1). Once the geometry matching had been achieved, patches of moving pixels (glacier ice, supraglacial debris) within the first (earlier) image were correlated within larger windows in the second (later) image to measure their displacement relative to the fixed features, giving the mean surface velocity (m d$^{-1}$) between the two acquisition dates. We only used the high-resolution (15 m) band 8 for velocity extraction, and a total of 16 image pairs were processed (Table 1). The error in the derived surface displacement is primarily determined by the accuracy of the co-registration (<15 m) between the repeat-pass images and the temporal separation between the image acquisitions. Estimated errors for the analysed image pairs vary between ∼0.03 and ∼0.2 m d$^{-1}$, depending on the time interval between acquisitions. (Due to a larger image separation for longer time-spans and a fixed location accuracy, the error decreases for an increasing observation period.) A large change in the dynamic state of the glacier was detected while inspecting a series of Landsat-7 scenes for general glacier evolution. Closer investigation revealed a sequential acceleration and slowdown of the glacier which is discussed here in more detail. The analysis focuses on a central flowline on the tongue of North Gasherbrum Glacier (Fig. 1). Along this flowline, surface displacements from the feature-tracking results were extracted. Examples for the surface displacement fields are shown in Figure 2. In general, valid displacements can be derived for the main glacier tongue below ∼5000 m elevation. The comparison of the quiescent phase with the main surge period shows that the lower tributaries are not involved in the surge activity. Usually successful tracking results provided surface displacements rather regularly along the lower part of the flowline, with only small gaps of several tens of metres. The calculated surface velocities could therefore be interpolated to provide continuous profiles. The surface geometry of the flowline shown in Figure 3 is based on the flowline location from Landsat-7 images and the Advanced Spaceborne Thermal Emission and Reflection Radiometer (ASTER) global digital elevation model (GDEM) (ASTER GDEM) is a product
Fig. 2. Surface displacements on North Gasherbrum Glacier resulting from the application of the feature-tracking algorithm on the Landsat-7 ETM+ scenes. Valid surface displacements are usually restricted to the main glacier tongue below 5000 m a.s.l. Here examples are given for (a) the quiescent stage, (b) the beginning of the surge, (c) the main phase of the surge and (d) the slowdown phase. Dates are dd/mm/yy.

The advance, 2003–07

Figure 4 shows velocity profiles from the years 2003–07. The velocities are calculated in terms of the available images, but each image pair covers ∼1 year, so the results represent annual mean velocities. For 2003/04 we only have valid results for a small segment between ∼8 and 10 km along the profile. The remaining profiles show a steady growth in velocity from the minimum in 2002/03 (0.38 m d⁻¹ or 139 m a⁻¹ at 6.5 km distance) to the maximum at 2006/07 (1.1 m d⁻¹ or 402 m a⁻¹ at 18.2 km distance). The feature-tracking results terminate at increasing distances downstream (the snout is relatively stationary near 21 km), which we take to represent the boundary between active and relatively stagnant ice. The increasing velocity leads to an enhanced transfer of ice downstream, and the glacier surface rises by ∼30 m in its downstream reaches. The magnitude of this increase in surface elevation was estimated from the comparison of photographs of the glacier taken in 2006 and the extent of the glacier at the left lateral moraine in the satellite image of 2007.

The retreat, 2007–09, 2002

Between 2007 (when the annual velocity peaks) and 2009 the velocity decreases. Figure 5 shows this decline, as well as the profile from 2001/02, which, since it is higher than the subsequent 2002/03 profile, suggests that it is also part of a declining phase, and thus that the behaviour may well be periodic. The unknown number of years between the 2009 profile and a subsequent 2002-like profile suggests a period of at least 8 years and probably somewhat longer. Taking into account the active phase of the surge, the typical period is probably about 15 years.

Summer 2009

While the velocity profiles in Figures 4 and 5 are relatively smooth, the one shown in Figure 6 has noticeable shortwave variation on a length scale of 1 km. This profile represents the average velocity over the late summer months August and September and the transition to the beginning of winter in early December 2009. In the first half of the period, strong surface melt can be expected, while in the second half water at the base of the glacier should still be available from the preceding melt period. Thus, the sliding velocity can be
expected to be large. A similar condition was also observed for the summer period (June–October) in 2008, but only a part of the profile could be analysed due to the quality of the feature-tracing results.

Frontal fluctuations

Glacier surges are usually thought to be connected with rapid advances of the glacier front. In the case of North Gasherbrum Glacier there is not much room for an advance. Between the glacier front and the opposite valley slope there was only a distance of 200–450 m in 2003, the year with the minimum velocity conditions. In 2007 this distance reduced to ~30–40 m in the centre and still ~400 m at the glacier margins. The maximum advance is observed in 2008, when the glacier at some locations seems almost to have made contact with the eastern valley slope. Compared to the total length of the glacier, this frontal advance of a maximum of ~200 m is rather small. There are also indications of possible glacier fluctuations from earlier remote-sensing information. Figure 7 shows the glacier snout in 1971, 1980 (both from Corona imagery) and 2007. In 1971 the minimum distance was ~80 m between the glacier and the eastern valley slope. The small channel along the centre of the glacier snout is ~90 m wide. In 2007 a similar channel exists, with a mean width of ~30–40 m. In 1980 the mean distance at the same location was ~200 m. If a periodic fluctuation of the glacier is assumed, the state in 1971 is probably very close to a maximum, while conditions in 1980 are similar to those in 2002/03, which are assumed to show a minimum state. This suggests that the periodicity of the fluctuations is roughly a decade, if we assume that the behaviour is indeed periodic (we emphasize that there is no direct evidence for this).

INTERPRETATION OF THE DATA

The velocity wave

Figure 4 represents a transition from a pre-surge velocity profile in 2002/03, which is more or less linearly declining from 9 to 16 km, to a surge velocity profile in 2005/06, which takes the form of a linearly increasing velocity from 10 to 16 km. Between 2006 and 2007, this profile advances as a wave, with the peak in the velocity advancing from 15.5 to 18.5 km, so the wave speed is ~3 km a⁻¹. The declining part of the profile represents the diffusive structure of a shock wave with width ~3 km.

Seasonal modulation

If we look closely at the 2006/07 profile in Figure 4, we can see that the average profile is modulated by a regular sequence of small-amplitude waves, with peaks at ~14, 16.5, 18.5, 20 and 20.8 km, so the wavelength is in the region of 2–2.5 km. Once we have recognized these modulations, we can see similar modulations in 2005/06 (at 12, 14, 15.5, 16.5 and 17.5 km) and even in 2004/05 (at 10.5, 12, 13.5, 15 and 16 km). Assuming these modulated peaks correspond to each other, they represent small-amplitude travelling modulation waves with speeds in the range 1.5–3.3 km a⁻¹.

Short waves

Figure 6, the only short time period profile, shows distinct variation on a short wavelength of ~1 km, which is absent on the longer time mean velocity profiles. Assuming these features are real, they might either represent dynamic wave features associated with compressional waves, or they might represent variations associated with underlying bed-slope variations in the form of riegels.

Upstream slowdown

All the velocity profiles exhibited a marked slowdown in an abrupt step, located (for 2002) at 10 km. The location of
this step is variable; in the years ordered 2003, 2004, ..., 2009, 2002, it is located approximately at 9, 10, 10, 10, 12, 11, 10 km; it thus appears to vary dynamically with the progression of the wave, advancing abruptly between 2006 and 2007 while the velocity wave propagates forward. One might suppose that the step is associated with one of the tributaries evident in Figures 1 and 3, located at ~10.1 and ~12.3 km along the flowline, and these do appear to be close to the range of the step, although the 2003 step is upstream of both. Alternatively, the slowdown could be caused by a steeper slope caused either by bed topography (but then it presumably should not move) or by drawdown of the ice during the surge (but then one expects upstream propagation of the step during the surge rather than an advance). Large variations in the surface slope are, however, not observed in the flowline geometry (Fig. 3).

A SIMPLE MODEL

When large changes occur on a glacier, such as described here, there are three obvious ways to interpret them. (1) They could be a transient response (e.g. as a kinematic wave) to a prolonged change in external conditions (e.g. a prolonged series of high-accumulation years). (2) They could represent a threshold phenomenon of a stable but excitable system. (3) They could represent a self-sustained oscillation, as a result of a change in velocity. Thus, in practice the only viable alternative to variations in sliding is by surface melting. A simple calculation using a constant activation energy, $Q^+$, for creep above $-10^\circ$C suggests that a surface velocity, $u$, due to shearing will be enhanced by $\Delta u$ given approximately by

$$\frac{\Delta u}{u} = \exp \left( \frac{Q^+ \Delta T}{RT_0^2} \right) - 1, \quad (1)$$

where the excess temperature, $\Delta T$, generated by refreezing of a surface melt of $\Delta h$ ice equivalent, redistributed over a glacier of depth $d$, is given by

$$\Delta T = \frac{L \Delta h}{c_p d^4}. \quad (2)$$

where $L$ is latent heat and $c_p$ is specific heat. Using values $Q^+ = 115 \text{ kJ mol}^{-1}$ (Cuffey and Paterson, 2010), $R = 8.31 \text{J mol}^{-1} \text{K}^{-1}$, $T_0 = 273 \text{K}$ and $L/c_p = 160 \text{K}$, we find

$$\frac{Q^+ \Delta T}{RT_0^2} \approx \frac{30 \Delta h}{d^2}. \quad (3)$$

To obtain the tenfold increase in velocity seen in the present data over a period of 4 years, we would thus need a melt of...
\[ \Delta h \approx d_t/30 \] over each of the four years. If \( d_t = 200 \text{ m} \), for example, this represents annual melting in excess of 6 m, which seems excessive. We therefore suppose that the velocity variations are due to sliding anomalies. If this is the case, it is sufficient to consider a model in which the velocity, \( u \), downstream is entirely by sliding, and this we do.

### The sliding law

The sliding law relates the basal stress, \( \tau \), to the velocity, \( u \), and the effective pressure, \( N \), which is the ice overburden pressure minus the water pressure in the subglacial drainage system. Lliboutry (1968, 1979) was an early advocate of the effects of subglacial cavitation, which led him to pose general laws of the form

\[
\tau = N f(\Lambda), \quad \Lambda = \frac{u}{\mathcal{N}^n},
\]

in which \( n \) is the exponent in Glen's flow law. Lliboutry found that \( f \) could be a unimodal (one-humped) function. Iken (1981) suggested a simple reasoning why this should be so. The result was subsequently confirmed in more elaborate calculations by Fowler (1986) and Schoof (2005). (The calculations are for Newtonian ice, \( n = 1 \), but one can infer the form of Equation (4) on dimensional grounds, assuming the bed roughness is sufficiently large that regelation can be ignored.)

An issue arises concerning the decreasing part of the sliding function, \( f \). Fowler (1987a) suggests that for real beds, with roughness at arbitrary large scales, \( f \) would continue to increase. Schoof's (2005) more precise calculations suggested that this could be an oversimplification, although he finally suggested a sliding law in which \( f \) increases towards a final maximum, thus corresponding to a frictional resistance, also advocated earlier by Lliboutry. In this paper we take the view that the presence of a real maximum in bed stress is associated with the catastrophic behaviour of hanging glaciers (Flotron, 1977; Pralong and Funk, 2006; Faillrettaz and others, 2008), and that where such behaviour does not occur, then either the bed is sufficiently rough that \( f \) increases, or else it effectively does so through the effects of side-wall friction (an extreme example of this is the behaviour of Ice Stream B, West Antarctica, where the driving stress exceeds the basal stress, and the balance is taken up by the lateral stresses; Whillans and Van der Veen 1997). If we suppose a power law, then the sliding law takes the form

\[
\tau = c u^r N^{1-n},
\]

where \( c \) and \( r \) are constant and we would suppose \( r < 1/n \). The form of this law receives some support from Budd and others (1979), Bindschadler (1983) and Iken and Bindschadler (1986). The shear stress is adequately represented by the expression (Nye, 1952)

\[
\tau = \rho g H (S - H_i),
\]

where \( H \) is ice depth, \( x \) is downstream distance, \( \rho_i \) is ice density, \( g \) is acceleration due to gravity and \( S \) is the mean valley slope; this expression neglects a further correction due to longitudinal stress gradients (Fowler, 1982).

### Drainage

The classical theory of subglacial drainage is due to Röthlisberger (1972), who described water flow through a channelized system by means of a set of equations which ultimately relate the effective pressure, \( N \), to the water flux, \( Q \). In the steady state, Fowler (1987b) showed that the solution could be adequately approximated, away from the glacier snout, by the algebraic relation

\[
N = \beta Q^{1/n},
\]

where \( n \) is the exponent in Glen’s flow law. This counter-intuitive result (flow rate is less at higher water pressure) is responsible for the idea of such a channelized system will consist of one, or at best a few, channels, because for two slightly dissimilar neighbouring channels, the smaller (at higher pressure) will drain into the larger. This property, that \( dN/dQ > 0 \), thus causes coarsening.

Lliboutry (1968) envisaged drainage through a system of linked cavities and Kamb (1987) devised a theory for such a flow, which importantly showed that water pressure increased with volume flux, so \( dN/dQ < 0 \) and the system is stable as a distributed system (as it must be, since cavities are distributed). In fact, Lliboutry's earlier theory can be used to illuminate the two types of drainage system. Lliboutry identified a shadowing function, \( s \), which we define to be the area fraction of the bed which is uncavitated. In keeping with the sliding theory discussed earlier, \( s \) is a monotonically decreasing function, \( s(\Lambda) \), with \( s(0) = 1 \). The effective pressure over the uncavitated part of the bed is then \( N/s \), and in a linked-cavity system we suppose that flow from cavity to cavity goes through orifices which are simply little R channels. If there are \( n_c \) such channels across the width of the glacier (essentially determined by the number of cavities), then the flow in each is \( Q/n_c \), so the analogue of Equation (7) is

\[
\frac{N}{s} = \beta \left( \frac{Q}{n_c} \right)^{1/n},
\]

Figure 8 illustrates the form of the drainage effective pressure given by Equation (8) relating effective pressure, \( N \), to water flow, \( Q \), through a field of linked cavities. To be specific, we define

\[
C = \ln \left( \frac{1}{s} \right),
\]

so that \( C \) is a monotonically increasing (from zero at \( \Lambda = 0 \)) function. We suppose that it saturates at large \( \Lambda \), indicating that complete flotation does not occur. Note that when \( N \) is large, \( \Lambda \) is small, and Equation (8) reverts to Equation (7).
The transition between effective pressures in terms of the ice sliding velocity. The R-channel and Kamb (K) linked-cavity values depend on the water flux, \( Q \), with the derivatives \( N'_R(Q) > 0 \) and \( N'_K(Q) < 0 \).

Hydrological switching

Supposing Figure 8 is appropriate, it should be interpreted as follows. The minimum of the curve is at \( \Delta = u/N^n = \Delta_c \), where \( \Delta_c \) is constant. In terms of determining \( N \), we must remember that \( Q \) is effectively prescribed, and \( u \) (and thus \( \Delta \)) is determined by the sliding law. As argued by Fowler (1987b), the implicit dependence of \( N \) on \( u \) leads to a multivalued relationship, as shown in Figure 9. The values of \( N \) are presumed dependent on the water flux, as indicated in Figure 8, so \( N_k \) is an increasing function of \( Q \), while \( N_N \) is a decreasing function of \( Q \).

The onset of a surge is associated with the gradual increase of depth during the quiescent phase. This leads to an increasing velocity and, if the accumulation rate is sufficiently large that \( u \) reaches the right-hand cusp in Figure 9, then the drainage system undergoes a transition to a linked-cavity system at lower effective pressure and the ice velocity increases. This is indicated in Figure 10, which shows how the multivalued drainage law leads to the multivalued relation between ice velocity and depth, even if the sliding law is single-valued, as in Equation (5).

The data in Figure 4 suggest that the transition to fast flow occurs over a period of some years, and it is necessary to consider how fast we might expect the transition between systems to occur. Firstly, a scaling analysis of the Nye (1976) version of Röthlisberger’s (1972) model shows that the ice closure equation can be written in an approximate dimensional form (Fowler, 2009):

\[
\frac{\partial S}{\partial t} = \left( \frac{f \rho_w g}{\rho_i L} \right) \frac{Q^3}{S^{4/3}} - KSN^3, \tag{10}
\]

where \( f \) is a friction factor, \( \rho_w \) is the density of water, \( g \) is acceleration due to gravity, \( \rho_i \) is ice density, \( L \) is latent heat and \( K \) is a viscous closure rate coefficient. The timescale, \( t_0 \), of closure is approximately \( t_0 \sim 1/KN^n \), and is \( \sim 1 \) day. Here, the cross-sectional area, \( S \), is related to the water flux, \( Q \), by \( S \propto Q^{3/4} \). A further timescale occurs in the mass-conservation equation for water, but this is a factor \( \varepsilon = \rho_w g h_0 \rho_i L \) smaller, where \( h_0 \) is the vertical descent over the water flow path. Typically \( \varepsilon \ll 1 \), so the water flux is given quasi-statically by integrating the surface meltwater source term, \( M \),

\[
\frac{\partial Q}{\partial x} = M, \tag{11}
\]

and the closure equation (Equation (10)) simply determines \( N \). In the time-dependent oscillations which occur during jökulhlaups, \( N \) and \( S \) interact through the provision of an evolution equation for \( N \) at the channel entry. Normally this is at the portal from an ice-dammed or subglacial lake, but it could equally well describe the initial drainage from the surface through crevasses and moulins. At the beginning of the subglacial channel system, we would then prescribe an equation (cf. Fowler, 2009)

\[
\frac{A_C}{\rho_w g} \frac{\partial Q}{\partial t} = M_0 - Q, \tag{12}
\]

where \( A_C \) is the effective crevasse/moulin surface area and \( M_0 \) is the surface meltwater supply rate to the channel inlet atrium. Choosing, somewhat imprecisely, \( A_C = 100 \, m^2 \), \( N \sim 10 \, bar \), \( Q \sim 1 \, m^3 \, s^{-1} \), this yields an inlet timescale:

\[
t_0 \sim \frac{A_C N}{\rho_w g Q} \sim 10^4 \, s. \tag{13}
\]

Thus all the timescales associated with adjustment of the channel system are small compared with the annual
timescale for meltwater supply variations. Consideration of the inter-cavity orifice transport in a linked-cavity system yields essentially similar results. A further timescale of relevance in the linked-cavity system is the adjustment time of the ice flow over cavities under changing effective pressures. This time is

\[ t_c \sim \frac{k_c}{u}, \]  

(14)

where \( k_c \) is the inter-cavity distance. For \( u = 100 \text{ m a}^{-1} \) and \( k_c = 20 \text{ m} \), this gives the longer timescale, \( t_c \sim 0.2 \text{ years} \). The timescale, \( t_W \), over which a local shutdown of the channel system will percolate across the width of a glacier might be expected to be somewhat longer than the ice-flow adjustment timescale, \( t_c \). Hewitt and Fowler (2008), following Walder (1986), also suggested a value \( t_W \sim 0.2 \text{ years} \).

We thus see that drainage transition is likely to occur on a timescale of weeks to months. This seems broadly consistent with observations of velocity and pressure variations over the course of a melt season (Kamb and others, 1985; Nienow and others, 1998), and so we shall suppose that the transition time between branches in Figure 9 (and thus also in Fig. 10) is of this order. The fact that the annual velocity variation in Figure 4 occurs over a timescale of 3 years is not inconmensurate with this, if we take into account that meltwater supply only occurs in the summer, so the drainage system has to rebuild itself each year. However, the main obvious cause of time variation in \( u \) arises from the fact that in a linked-cavity system \( u \) increases with water flux, \( Q \), which itself increases with time during the melt season.

Surge model

The model of the surge of a glacier is based on that of Kamb and others (1985), as elaborated by Fowler (1987b). To the above relations between basal stress, drainage effective pressure and sliding velocity we add the equation of conservation of mass in the form

\[ H_t + (Hu)_x = a, \]  

(15)

where the subscripts denote partial derivatives, \( a \) is the accumulation rate and we suppose for simplicity that all motion is by sliding. Our discussion of a surge follows that of Fowler (1987b, 1989) and is summarized here. As the glacier thickens during the pre-surge quiescent phase, \( H \) approaches \( H_+ \) in Figure 10, and when it reaches it, there is a transition of the drainage system to a distributed system on the part of the glacier (the reservoir region) where \( H > H_- \). This activated region shifts to the upper branch of Figure 10, and the resultant rapidly moving ice in the reservoir region slumps forward as a wave, and its height lowers as a consequence. This may or may not lead to an advance of the snout, depending on the volume of ice above the critical level, \( H_- \), in the reservoir area and the size of the downstream receiving area (Fig. 11).

To this description we now add the effect of a water flux, \( Q \), which increases downstream. Adopting Equation (6) in the form \( \tau = H \), then from Equation (5) the sliding law is

\[ u \approx \left( \frac{H}{c} \frac{1}{N^1/\beta} \right)^{1/r}. \]  

(16)

For Röthlisberger channels, we might suppose (Equation (7)) that the effective pressure, \( N \), is determined by

\[ N \approx \beta Q^{1/4n}, \]  

(17)

while for the distributed drainage system, we might take for small (but not very small) values of \( N \) (Fig. 8) \( C \approx A \), and thus, from Equation (8),

\[ u \approx \left( \frac{H}{c} \frac{1}{\beta^{1/n}} \right)^{1/r} \frac{1}{\ln \left( \frac{Q}{N} \right)} \]  

(18)

and we approximate this by

\[ u \approx \frac{1}{4n} \ln Q. \]  

(19)

From these, together with Equation (16), the channel \((R)\) and linked-cavity \((K)\) sliding laws relating \( u \) to depth, \( H \), and water flux, \( Q \):

\[ u \approx \left( \frac{H}{c} \frac{1}{\beta^{1/n}} \right)^{1/r} \frac{1}{\ln \left( \frac{Q}{N} \right)} \]  

(R),

\[ u \approx \left( \frac{H}{c} \right)^{n/4} \frac{1}{4n} \ln Q \]  

(K).  

(20)

In the absence of specific information on water flow and sliding parameters, we assume generally that \( Q \) increases with downstream distance, \( x \), and thus the R-channel sliding law has \( u \) decreasing with \( x \), while the linked-cavity sliding law has \( u \) increasing with \( x \). For illustrative purposes we take

\[ u \approx A_k H x \]  

(R),

\[ u \approx A_k H^m x \]  

(K).  

(21)

This choice is partly motivated by Figure 4, where the 2002/03 and 2006/07 profiles suggest \( A_k H^m = 0.1 \times 10^4 \text{ m}^3 \text{ d}^{-1} \) and \( A_k H = 0.72 \times 10^{-4} \text{ m}^2 \text{ d}^{-1} \). We now interpret Figure 4 as follows. The reservoir area is between \(~10 \text{ and } 15 \text{ km} \) (central part of the ablation area) and between 2003 and 2006 the velocity rises from \( u_k \approx 1/x \) to the activated velocity, \( u_k \approx x \), if the origin is taken at \(~4 \text{ km} \) (roughly the position of the equilibrium line). This rise propagates somewhat further back, and also as soon as the velocity commences its ascent, a shock wave begins to propagate forward: already by 2005 it had advanced to \(~17 \text{ km} \).
Velocity wave

We can provide some information about the drawdown and the shock speed as follows. Based on Equation (21), \( H \) satisfies the approximate equation behind the surge front

\[
H_t + \left( A_k H^{m+1} \right)_x = -|a|
\]

(22)
during the surge (all the data are in the ablation zone, the equilibrium line being at \( \sim -4 \) km). Observation of a net rise in elevation downstream (between 17 and 19 km) of \( \sim 30 \) m suggests that

\[
\Delta H = (H_k - H_-) \lesssim 30 \text{ m},
\]

(23)
whereas we surmise that the depth, \( d \), of the glacier is \( \sim 200 \) m. An estimate for the advance of the surge front, \( \Delta x_t \), can then be found by elementary geometrical considerations. If the reservoir area has length \( \Delta x \) and we assume a constant pre-surge surface slope, \( S \), downstream of this, then we have the approximate relation

\[
\frac{1}{2} \Delta x \Delta H \approx \frac{1}{2} S \Delta x_t^2.
\]

(24)
If we take \( \Delta x = 5 \) km, \( \Delta H = 30 \) m, \( S = 0.04 \) (based on a 200 m drop over 5 km), then we calculate

\[
\Delta x_t = \left( \frac{\Delta x \Delta H}{S} \right)^{1/2} \approx 2 \text{ km}.
\]

(25)
This, obviously, is very crude, but it does provide an explanation for why the surge does not cause a real advance of the glacier.

**Drawdown**

We write Equation (22) in the form

\[
H_t + (m + 1)A_k H^{m+1} H_x = - \left( |a| + A_k H^{m+1} \right).
\]

(26)
If we put

\[
H = H_- + \Delta H \eta
\]

(27)
(\( \eta \) is dimensionless and \( O(1) \)) then, since \( \Delta H \ll H_- \), the rate of drawdown is given by

\[
- \eta_t \approx \frac{GH_-}{\Delta H},
\]

(28)
where

\[
G = A_k H^{m+1},
\]

(29)
assuming \( |a| \ll GH_- \). From Figure 4, we can estimate \( G \approx 2.63 \times 10^{-2} \) m a\(^{-1} \), so \( GH_- \approx 5 \) m a\(^{-1} \), compared with an ablation rate of \( 1-2 \) m a\(^{-1} \). The timescale for drawdown of \( \eta \) by \( O(1) \), and thus the duration of the surge, is then

\[
\tau_d \approx \frac{\Delta H}{GH_-} \approx 5.7 \text{ years},
\]

(30)
especially as observed (the velocity increases from 2004 to 2007 and declines from 2007 to 2009).

**Shock speed and width**

The speed of the advancing shock front at \( x = x_t \) in which the velocity decreases from its surging value to essentially zero, is given by the jump condition

\[
x_t = \frac{\left| H_\| \right|}{\left| H \right|} \approx \frac{H_- u_-}{\Delta H} \approx \frac{GH_- x_t}{\Delta H}.
\]

(31)
For values \( u_- \approx 1 \) m d\(^{-1} \) and \( \Delta H/H_- \approx 0.15 \), this gives a wave speed of \( 2.4 \) km a\(^{-1} \), as observed. Moreover, the wave-front position accelerates, since by solving Equation (31) we have

\[
x_t \sim \exp \left( \frac{GH_- t}{\Delta H} \right),
\]

(32)
and this acceleration can also be seen in Figure 4.

Shocks are discontinuities, but in reality are smoothed out by diffusive processes. Ordinary surface waves are smoothed by the term involving the deviation of the surface slope from the mean slope in Equation (6). In the present situation, the relaxation time, \( t_W \), for transition between differing drainage systems plays a key role. Suppose that the effective pressure satisfies an equation of the form:

\[
l_W N_t = N_{eq}(\Lambda) - N.
\]

(33)
In the shock, we put

\[
x = x_t + (\Delta X) X, \quad H = H_- + \Delta H \eta,
\]

(34)
where \( \Delta X \) is the shock width; note that \( \eta \) and \( X \) are dimensionless. It follows from Equation (33) that the drainage transition occurs over the dimensionless range \( X = O(1) \) if we choose

\[
\Delta X = \eta \tau_W,
\]

(35)
where \( \eta = \hat{x} \) is the shock speed. If we take \( \eta = 2.4 \) km a\(^{-1} \) and \( \tau_W = 3 \) years, as suggested by Figure 4, then \( \Delta X \approx 7 \) km. This compares favourably to the apparent shock widths in Figure 4, which (by extrapolating the velocity in the front down to zero) take the apparent values 2, 3, 4.5 and 6 km in the years 2003, 2005, 2006 and 2007; the increase is associated with the increase in \( \eta \) as the front progresses.

To see that a shock structure does exist in the model, we write the mass-conservation equation in the form

\[
\frac{\partial H}{\partial t} + \frac{\partial}{\partial x} \left[ A_k H^{m+1} \left( 1 - \frac{1}{5} \frac{H}{H} \right)^m x T(X) \right] = a,
\]

(36)
where the function \( T(X) \) represents the transition from distributed to channelized drainage near the shock front. Ignoring the velocity in front of \( x_t \), we can take \( T \) to be a monotonically decreasing function of \( X \), with \( T(\infty) = 1, \quad T(-\infty) = 0 \). The slope-dependent term represents the normal surface diffusive effect present in Equation (6). Substituting Equation (34) into Equation (36) and retaining leading-order terms, we obtain an equation whose first integral is

\[
\eta = (1 - \delta \eta X)^m T(X),
\]

(37)
with boundary conditions

\[
\eta(-\infty) = 1, \quad \eta(\infty) = 0.
\]

(38)
We have used the definition of the shock speed given by Equation (31), and neglected ablation on the basis that \( (\Delta x)/(\eta \Delta X) \approx 1 \), as is the case. The parameter \( \delta \) is defined by

\[
\delta = \frac{\Delta H}{\Delta X}.
\]

(39)
and for the values $\Delta H \sim 30\text{ m}$, $S \sim 0.04$, $\Delta X \sim 7\text{ km}$, this gives $\delta \sim 0.1$, although it is 0.3 for the 2003 width of 2 km. For small $\delta$, the solution is apparently $\eta \approx T(x)$, and this can be confirmed by consideration of Equation (37), where a graphical analysis of trajectories of $w = \eta/T$ shows that a solution of Equations (37) and (38) exists for all positive $\delta$.

**Modulation waves**

Finally, we turn to the seasonal modulation waves discussed above. Based on our inspection of Figure 4, we have analysed these data in more detail by looking at the variations of the velocity from the local spatial average. The results are shown in Figure 6, where four (or possibly five) clear amplitude peaks can be traced from 2005 to 2007. The waves move forward at an accelerating rate, just as the shock front does. The initial wavelength is $\sim 2.5\text{ km}$.

The most obvious explanation for this variation is in the seasonal variation of water supply. Roughly speaking, the coefficient $A_k$ in Equation (21) (cf. Equation (20)) represents the meltwater supply. The simplest modification of Equation (21) to allow for this is to assume that $A_k = A_k^0 + A_k^1 x$, where $A_k^0$ is a suitable length scale (e.g. the length of the ablation zone). Approximately, the surface perturbation, $\eta$, satisfies

$$\eta + G \eta = -\frac{G}{\nu},$$

where

$$\nu = \frac{\Delta H}{H^*}. \quad (43)$$

We write

$$\eta = \tilde{\eta} + \phi, \quad G = \tilde{G} + \nu g'(t),$$

where $\tilde{G}$ is the time average of $G$ and

$$\tilde{\eta} = \frac{\tilde{G}}{\nu}, \quad \phi \approx -g'(t),$$

$$\phi + \tilde{G} \phi \approx -g'(t), \quad (46)$$

and a suitable boundary condition follows from the prescription that $H = H^*$ at the head of the reservoir region. In Figure 4, this is at $\sim 10\text{ km}$, so if we take $l = 10\text{ km}$, then we put $\eta = 0$ and thus also $\phi = 0$ at $\xi = 0$. The solution of Equation (46) is thus

$$\phi = -g(t) + \tilde{G} \left( t - \frac{\xi}{\tilde{G}} \right), \quad (47)$$

At a fixed time, the surface is periodic in $\xi$ with a period $\Delta \xi = G \times 1\text{ years} \approx 2.63 \times 10^{-2}$, and thus the actual spatial period is $\Delta x = (m+1)\Delta \xi \approx 0.26(m+1)\text{ km}$, which corresponds to the observed period of 2.5 km if $m \approx 9$ (if $x = 10\text{ km}$; $m \approx 5$ if $x = 15\text{ km}$). This is a rather high value, but may be associated with our particular assumptions about the sliding and drainage laws. In particular, the exponent $m$ in Equation (20) is based on the sliding and drainage laws associated with viscous ice deformation over hard beds, whereas those associated with deformation of subglacial sediment may support a more plastic (high $m$) rheology (Kamb, 1991).

Additionally, the wave crests move at constant speed in the $\xi$ plane, $\xi = G t$, and thus $x \approx \exp[(m+1)\xi t]$, consistent with the acceleration shown in Figure 12.

**CONCLUSIONS**

Glacier surges occur regularly in the Karakoram, even though most of these surges go unnoticed in remote areas. Nonetheless, such processes can pose a serious threat to humans by blocking valleys and impounding large amounts of water that can be suddenly released by a breach of the ice dam. North Gasherbrum Glacier clearly has the potential to block the Shaksgam valley, because even a small advance of a few hundred metres is sufficient. Therefore the observation that this glacier probably shows periodic fluctuations is somewhat disturbing.

Our study shows that the dynamic reaction of a glacier can be well analysed if a sufficient number of remote-sensing observations are available. Another prerequisite for such an analysis is the availability of an appropriate digital elevation model (DEM). For the rather smooth and large glacier tongue of North Gasherbrum Glacier the elevation information from the ASTER GDEM is sufficient for the analysis. In the case of smaller glaciers, the planned DEM based on the TanDEM-X mission is keenly awaited by the glaciological community.
We have provided an analytic interpretation of the remote-sensing imagery in terms of a postulated surge theory for North Gasherbrum Glacier, which includes the influence of basal water flux and the specific geometry on the changes in ice flux. Because very little is known of the glacier, it must be emphasized that this theory is hardly at the predictive stage. Instead, what we have tried to do is to interpret the data in terms of one particular theory of glacier dynamics, based on simple yet sophisticated concepts of glacier sliding with cavitation and subglacial hydrological switching. Using very simple quantitative arguments, we are able to explain in detail the form and propagation of the velocity wave, and even the modulative effects of annual meltwater supply variation. The only inference of our theory that may be at odds with expectation is the requirement of a drainage-switching timescale of 3 years, as opposed to the expected value of 0.2 years. This may be associated with the confounding effects of annual shutdown and restart, or it may be associated with a longer timescale associated with cross-glacier hydraulic transition. Equally, however, it may indicate that the premise of our theory is fundamentally flawed, and that the cause of the velocity fluctuations lies elsewhere. Even if sliding and drainage are responsible, the particular assumptions concerning the sliding law and hydraulic switching are very vague and unconstrained. At best, the present results only indicate a possible physical scenario for the observations.

It seems that, for the given amplitudes of velocity increase and the observed glacier geometry, massive advances of the glacier snout are not very likely. The ratio between reservoir and receiving area favours a rapid mass shift without a strong change in the snout position. Changes in the putative hydraulic system due to enhanced ice melt (if summer temperatures continue to rise), or changes in the ice geometry due to a higher mass flux from the accumulation area (if the higher winter precipitation, observed by Archer and Fowler (2004) continues) could change the supposed surge characteristics of this glacier towards those of a glacier whose length oscillates periodically.

ACKNOWLEDGEMENTS

A.C.F. acknowledges the support of the Mathematics Applications Consortium for Science and Industry (www.macsi.ul.ie) funded by the Science Foundation Ireland mathematics initiative grant 06/MI/005. The free use of Landsat-7 and Corona data from the US Geological Survey for this analysis is greatly appreciated. C.M. and A.L. thank EvK2-CNR and the Geographic Institute ‘Ardivo Desio’ of the University of Milan for generous support. We thank F. Ng and K. Hewitt for their thorough reviews and constructive suggestions.

REFERENCES


Mayer and others: Surge of North Gasherbrum Glacier


MS received 23 March 2010 and accepted in revised form 21 January 2011